

# Magnetic Reconnection

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# Outline

A broad view on magnetic reconnection

Fundamental problems & research

- Reconnection rate problem
- Three-dimensional (3D) nature of reconnection

Summary

# Background

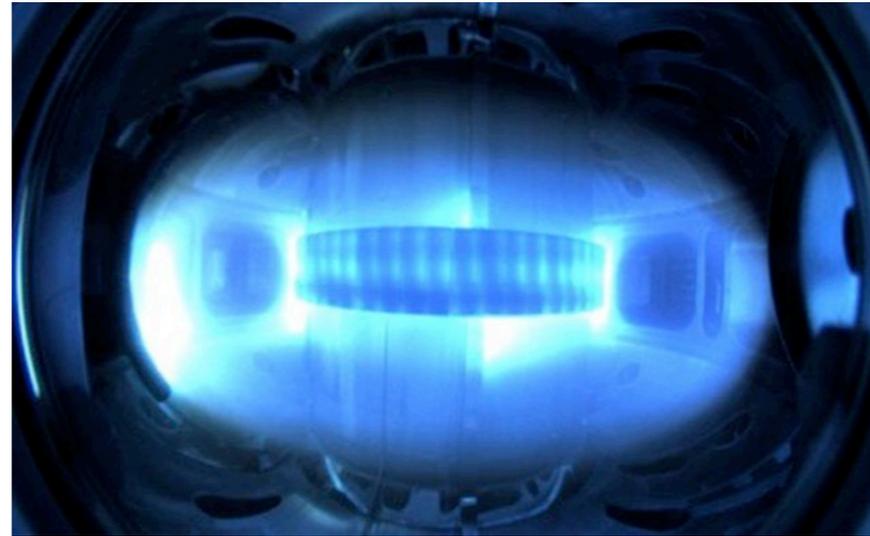
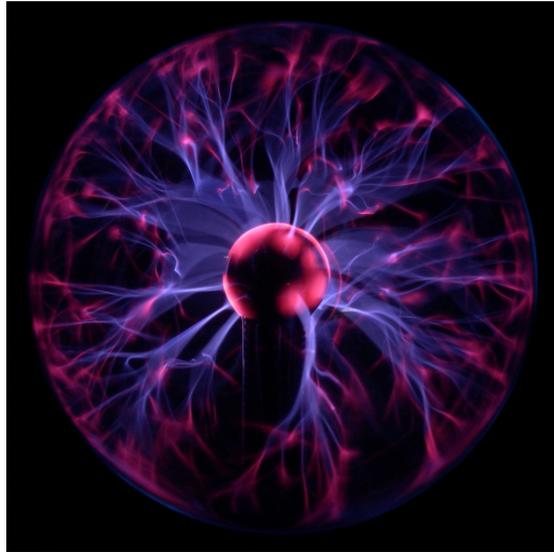
- All about the geometry & topology of magnetic field lines

# Plasmas

4th state of matter  
> 99% of visible universe\*

Fusion device

Plasma Lamp



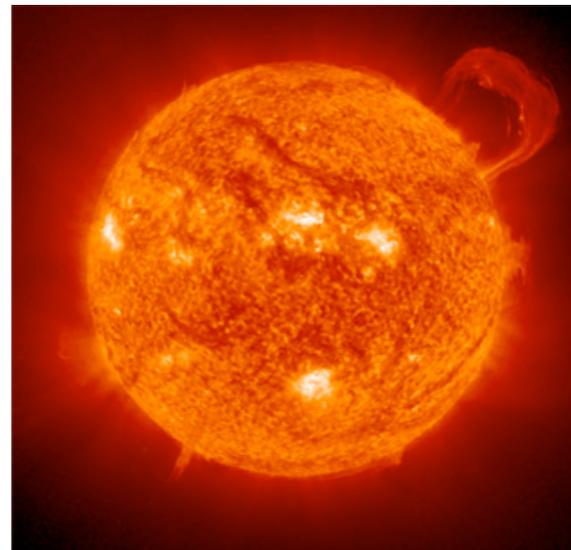
Lightning



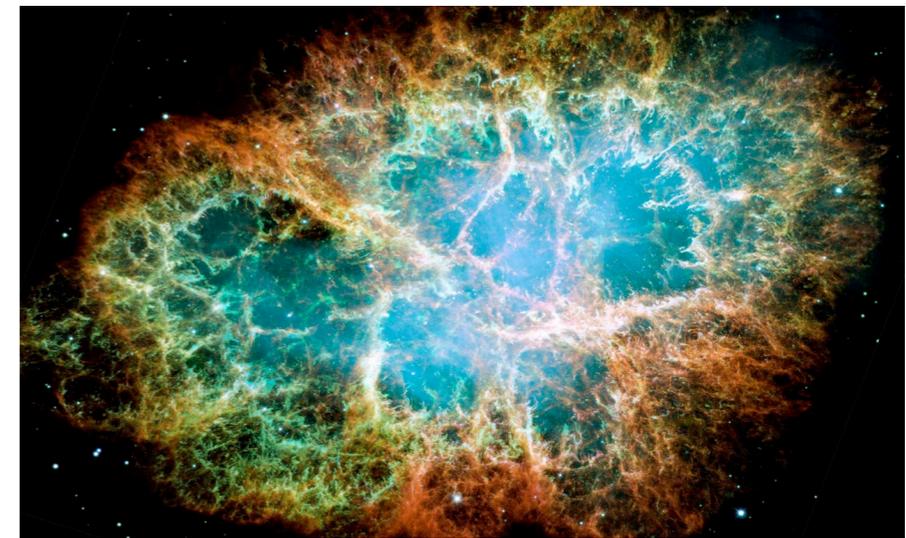
Aurora Borealis



Solar Eruption

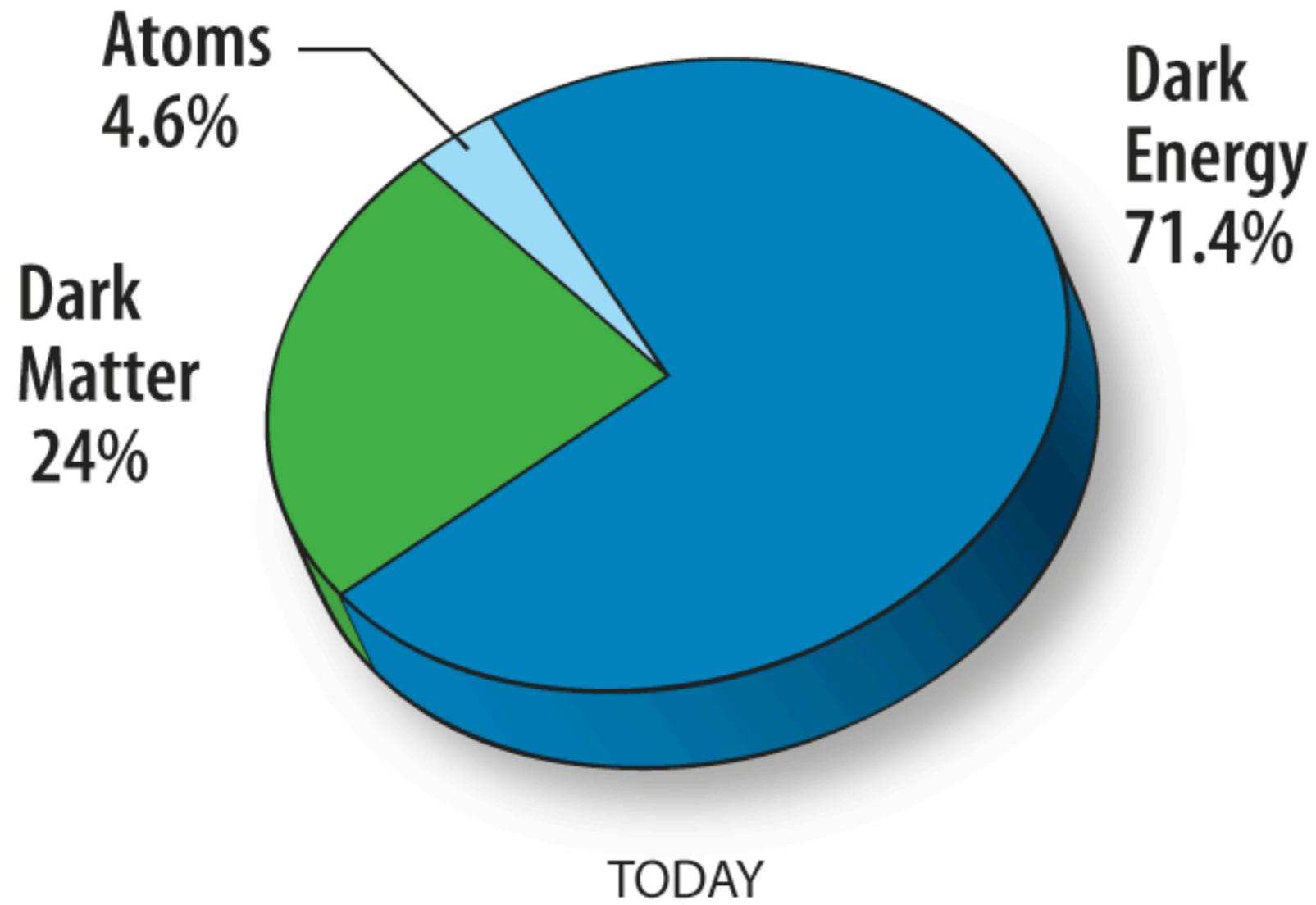


Nebula

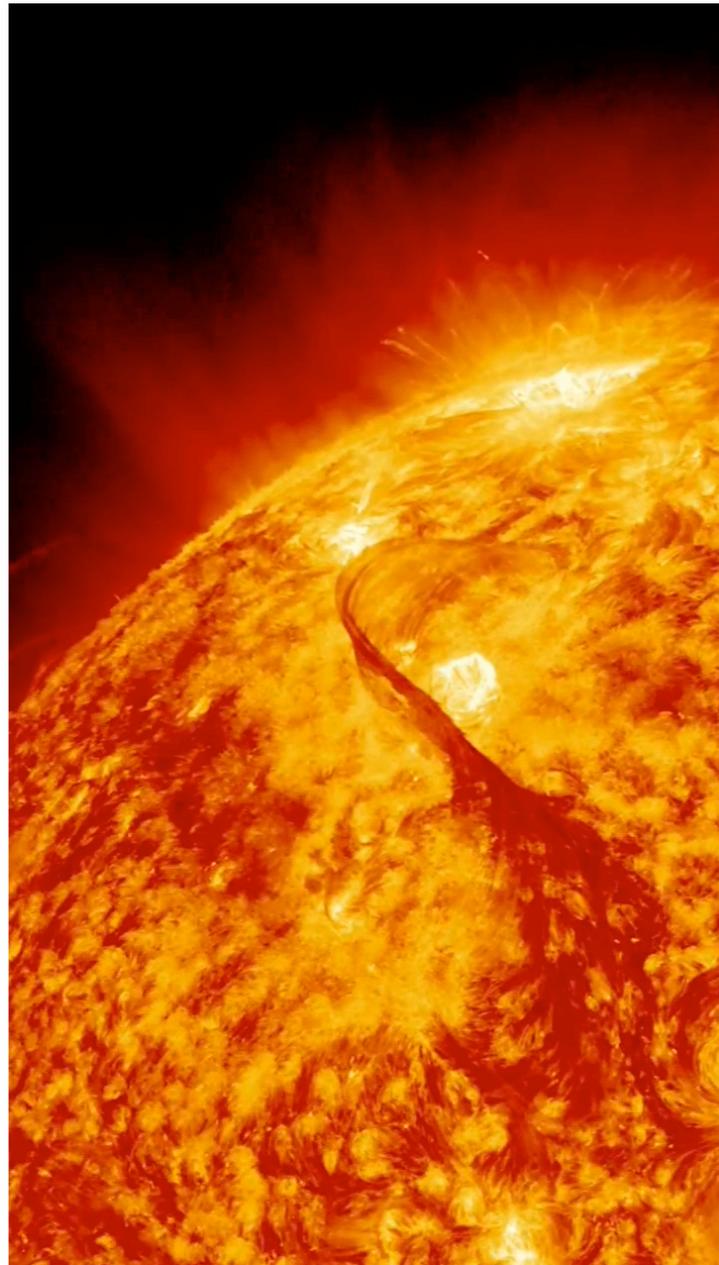


- Interaction between lots<sup>n</sup> of charge particles + electromagnetic fields
  - complicated & nonlinear!!
- Long range electromagnetic interaction!!
  - the evolution CANNOT be described by thermodynamics.

**\*Footnote**

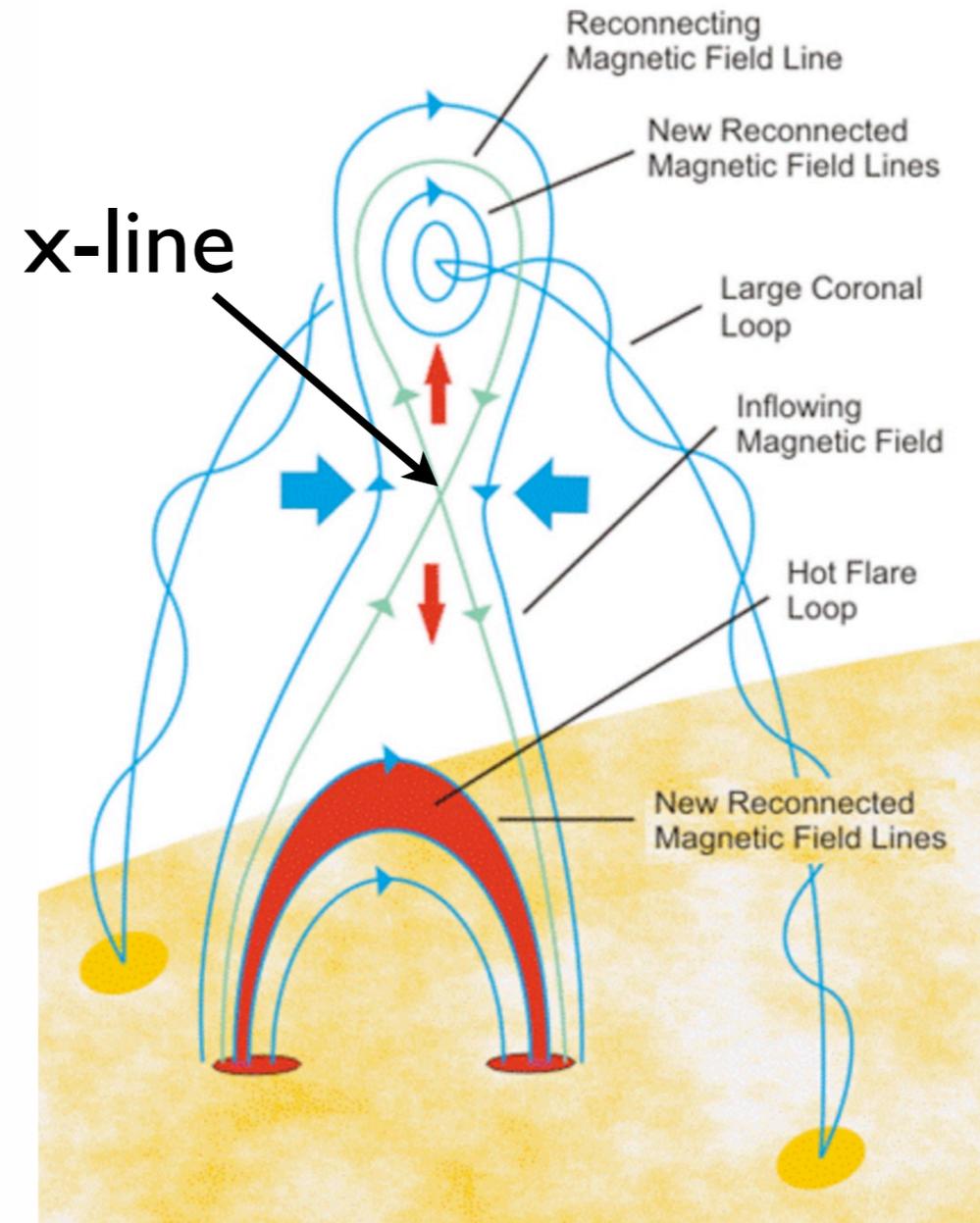


# Solar Eruption



(Courtesy of SDO mission)

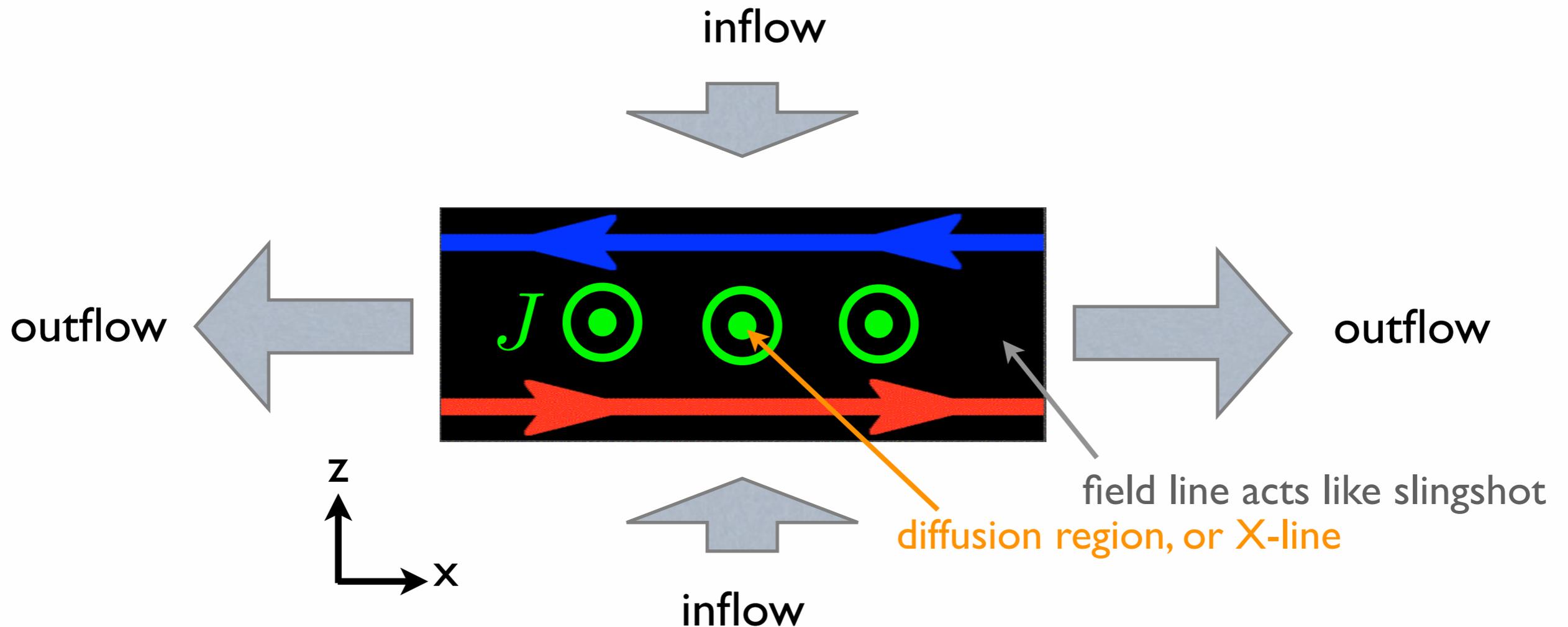
B~200 Gauss  
T~3,000,000 K



(Courtesy of NASA)

- Energy up to  $10^{32}$  ergs is released in  $\sim 20$  mins  
-- 40 billion atomic bombs!
- Matter up to  $10^{10}$  tons is erupted.

# Magnetic Reconnection?



diffusion region, or X-line

field line acts like slingshot

1. Inflow brings in magnetic flux
2. Field lines break & reconnect
3. Reconnected field line shoots out plasma
4. Pressure drop sucks in plasma inflow

(frozen-in)

(frozen-in is violated !!)

(frozen-in)

1. Inflow brings in magnetic flux

(frozen-in)

2. ....

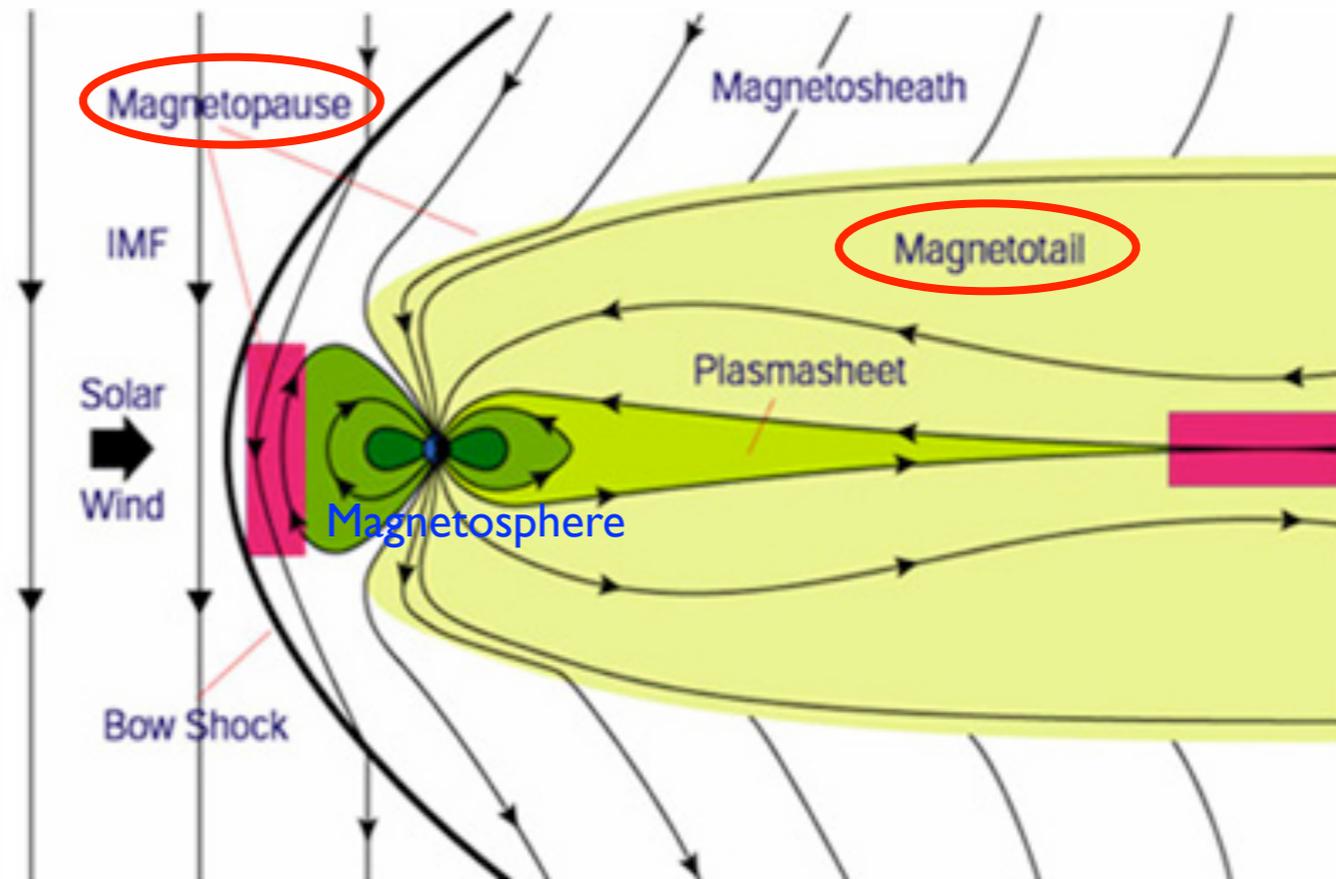
3. ...

**A self-driven process!!!**

# Earth's magnetosphere



IMF  
(Interplanetary  
Magnetic Field)



magnetosheath

$$B \sim 20nT$$

$$n \sim 15cm^{-3}$$

magnetosphere

$$B \sim 60nT$$

$$n \sim 0.5cm^{-3}$$

magnetotail

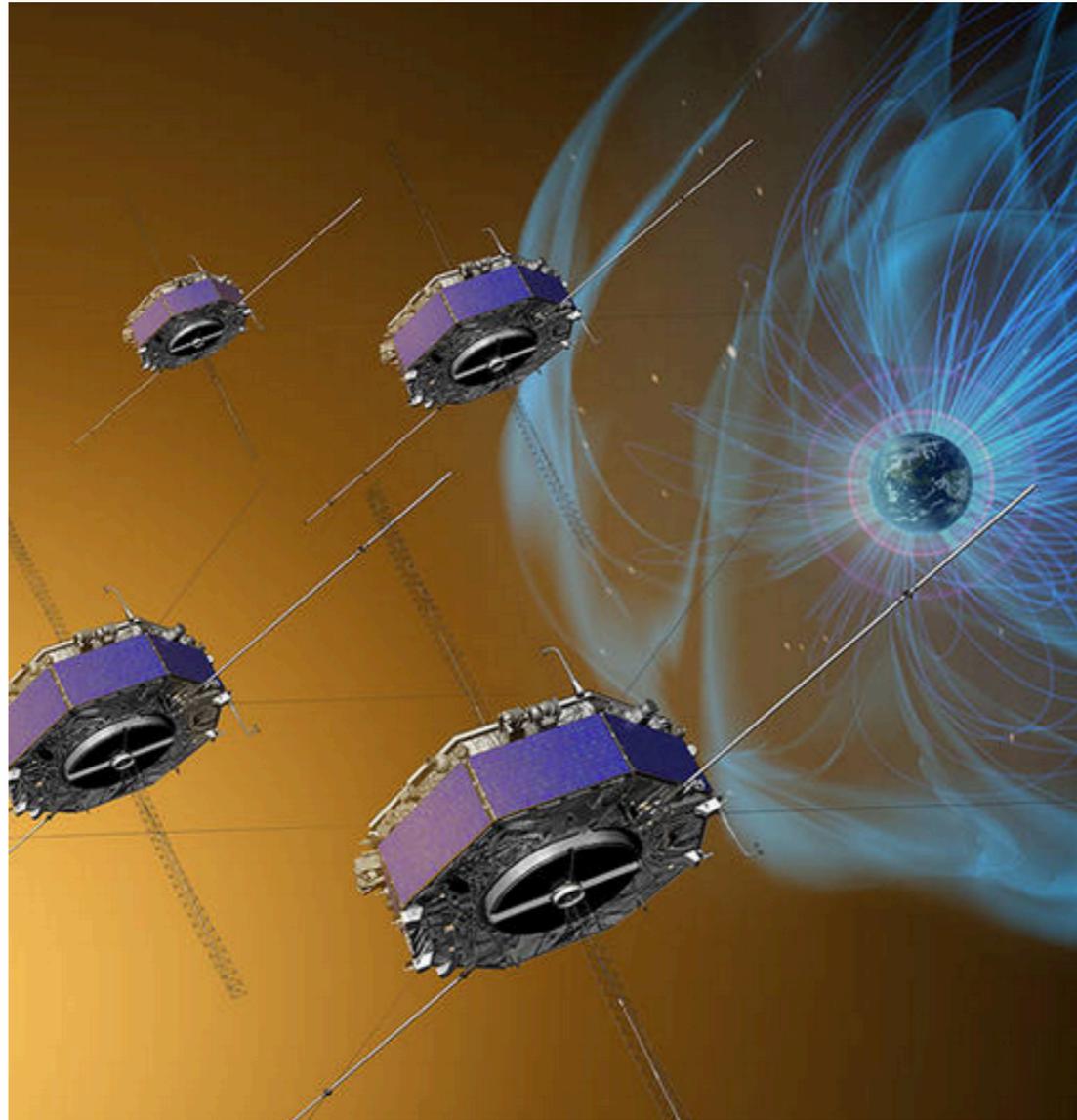
$$B \sim 20nT$$

$$n \sim 0.01cm^{-3}$$

- Reconnection occurs at both the magnetopause & magnetotail.
- Reconnection at the magnetotail drives magnetospheric substorm & enhances aurora.

# A billion \$ NASA mission designed to study magnetic reconnection

## Magnetospheric Multiscale Mission (MMS)

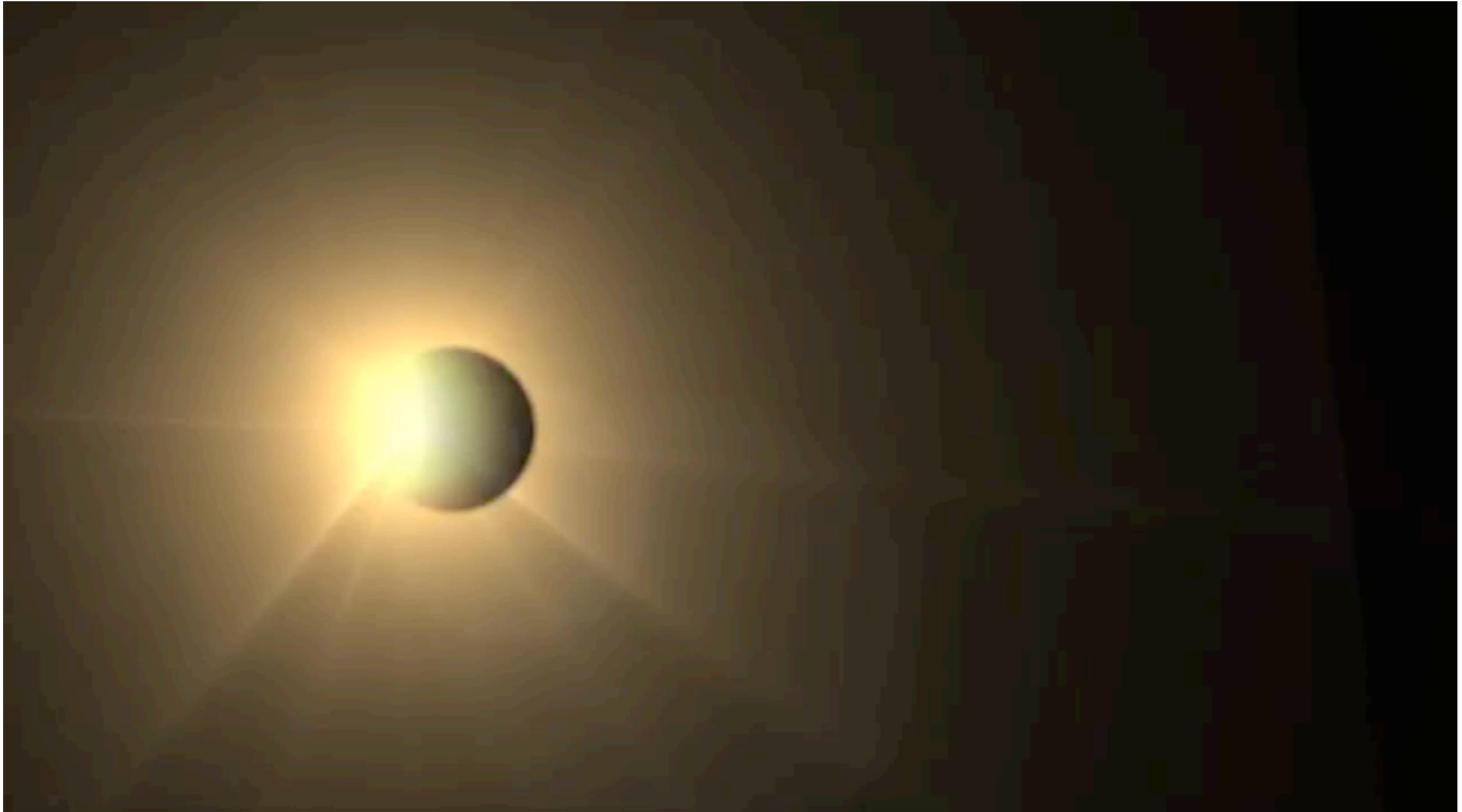


<http://mms.gsfc.nasa.gov>

tight tetrahedron formation: separation down to 7 km!  
100x faster for electrons measurement (30 ms)  
30x faster for ions measurement (150 ms)

- MMS leads us into a stage where the **electron-scale** physics of magnetic reconnection, **in nature**, can be resolved in an unprecedented manner!!

# The trailer of MMS ...



Cite as: J. L. Burch *et al.*, *Science*  
10.1126/science.aaf2939 (2016).

# Electron-scale measurements of magnetic reconnection in space

J. L. Burch,<sup>1\*</sup> R. B. Torbert  
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Yu. V. Khotyaintsev,<sup>13</sup> P.-A.  
Goldstein,<sup>1</sup> J. C. Dorelli,<sup>5</sup> L.  
Cohen,<sup>10</sup> D. L. Turner,<sup>15</sup> J. I.  
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PRL 116, 235102 (2016)

PHYSICAL REVIEW LETTERS

week ending  
10 JUNE 2016

## Magnetospheric Multiscale Satellites Observations of Parallel Electric Fields Associated with Magnetic Reconnection

R. E. Ergun,<sup>1,2</sup> K. A. Goodrich,<sup>1,2</sup> F. D. Wilder,<sup>2</sup> J. C. Holmes,<sup>1,2</sup> J. E. Stawarz,<sup>1,2</sup> S. Eriksson,<sup>2</sup> A. P. Sturmer,<sup>1,2</sup> D. M. Malaspina,<sup>1</sup> M. E. Usanova,<sup>1</sup> R. B. Torbert,<sup>3,4</sup> P.-A. Lindqvist,<sup>5</sup> Y. Khotyaintsev,<sup>6</sup> J. L. Burch,<sup>4</sup> R. J. Strangeway,<sup>7</sup> C. T. Russell,<sup>7</sup> C. J. Pollock,<sup>8</sup> B. L. Giles,<sup>8</sup> M. Hesse,<sup>8</sup> L. J. Chen,<sup>9</sup> G. Lapenta,<sup>10</sup> M. V. Goldman,<sup>11</sup> D. L. Newman,<sup>11</sup> S. J. Schwartz,<sup>2,12</sup> J. P. Eastwood,<sup>12</sup> T. D. Phan,<sup>13</sup> F. S. Mozer,<sup>13</sup> J. Drake,<sup>9</sup> M. A. Shay,<sup>14</sup> P. A. Cassak,<sup>15</sup> R. Nakamura,<sup>16</sup> and G. Marklund<sup>5</sup>

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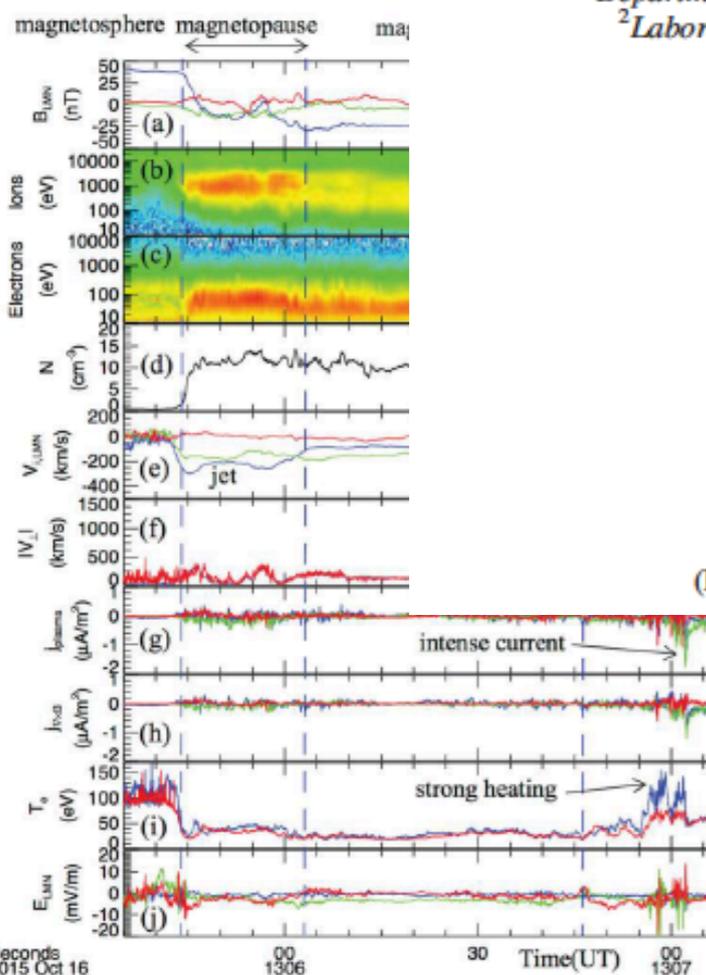
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AGU PUBLICATIONS

JGR

Journal of Geophysical Research: Space Physics

RESEARCH ARTICLE

10.1002/2017JA024004

Special Section:

Magnetospheric Multiscale (MMS) mission results throughout the first primary mission phase

Electron diffusion region during magnetopause reconnection with an intermediate guide field: Magnetospheric multiscale observations

L.-J. Chen<sup>1,2</sup> , M. Hesse<sup>1</sup> , S. Wang<sup>1,2</sup> , D. Gershman<sup>1,2</sup> , R. E. Ergun<sup>3</sup> , J. Burch<sup>4</sup> , N. Bessho<sup>1,2</sup> , R. B. Torbert<sup>4,5</sup> , B. Giles<sup>1</sup> , J. Webster<sup>6</sup> , C. Pollock<sup>7</sup> , J. Dorelli<sup>1</sup> , T. Moore<sup>1</sup> , W. Paterson<sup>1</sup> , B. Lavraud<sup>8,9</sup> , R. Strangeway<sup>10</sup> , C. Russell<sup>10</sup> , Y. Khotyaintsev<sup>11</sup> , P.-A. Lindqvist<sup>12</sup> , and L. Avanov<sup>1,2</sup>

# Briefing of MMS mission

02/25/2015 @ NASA headquarter



Moderator

NASA  
Headquarter

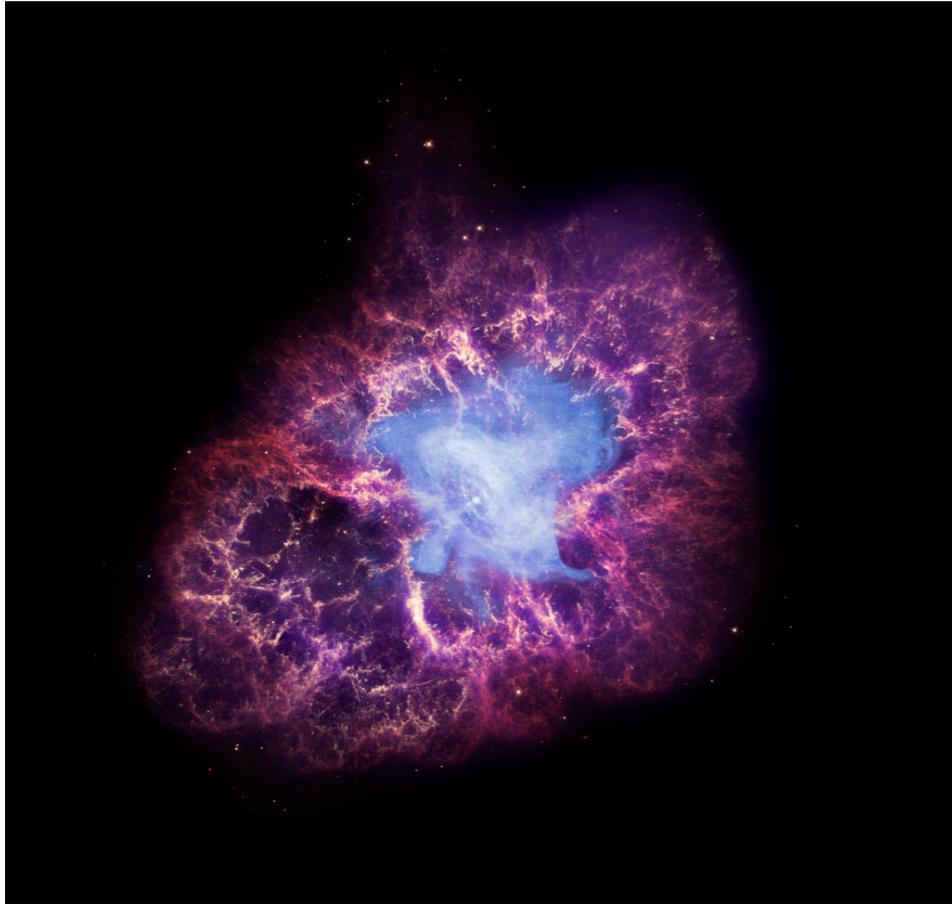
Project  
PI

Project  
Scientist

Guest  
Researcher

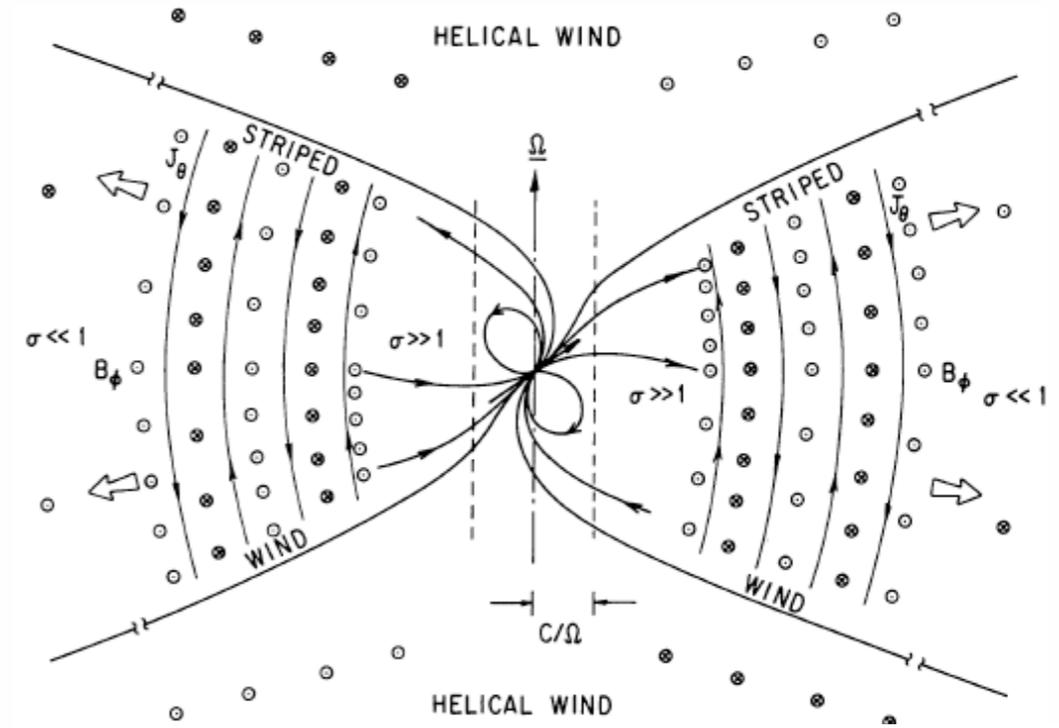
# Astrophysical systems

## Superflares @ Crab Nebula

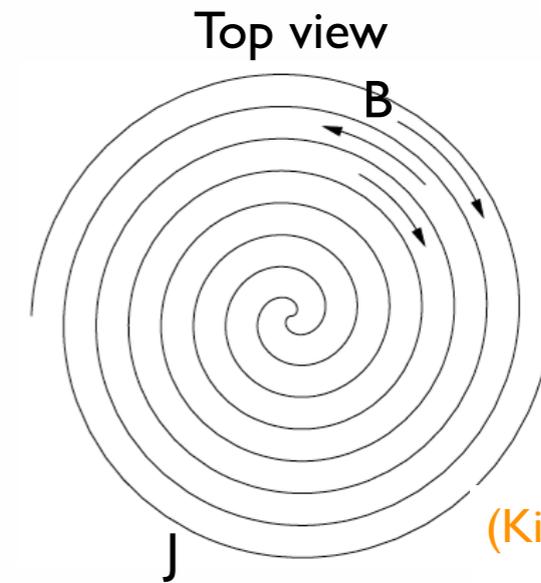


(Striani et al. 2011)

time scale ~days



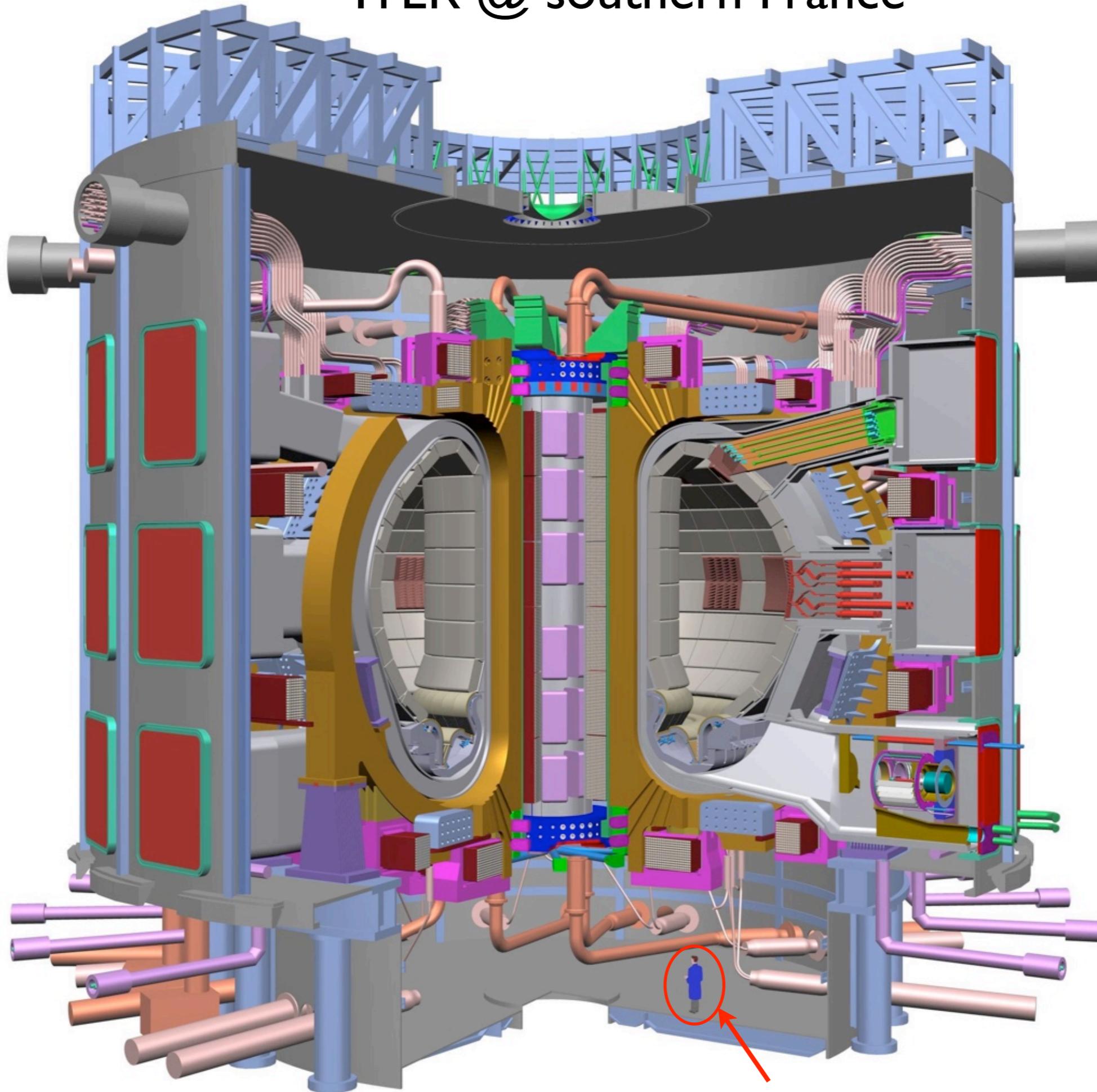
(Coroniti 1990)



(Kirk & Skaeraasen 2003)

- Strong magnetic fields are dissipated quickly! ( $\sigma$ -problem)
- **Relativistic** reconnection could be important, and at other places like:
  - Jets from active galactic nuclei (AGN)/ black holes
  - Gamma-Ray bursts (GRBs)

# ITER @ southern France



# (fake) Fusion reactors in Hollywood

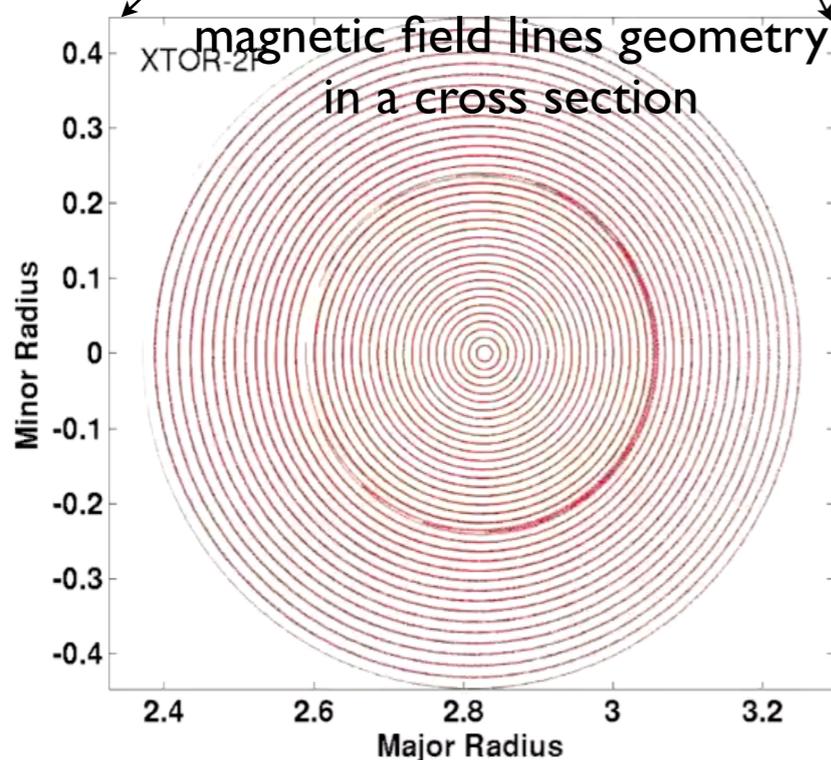
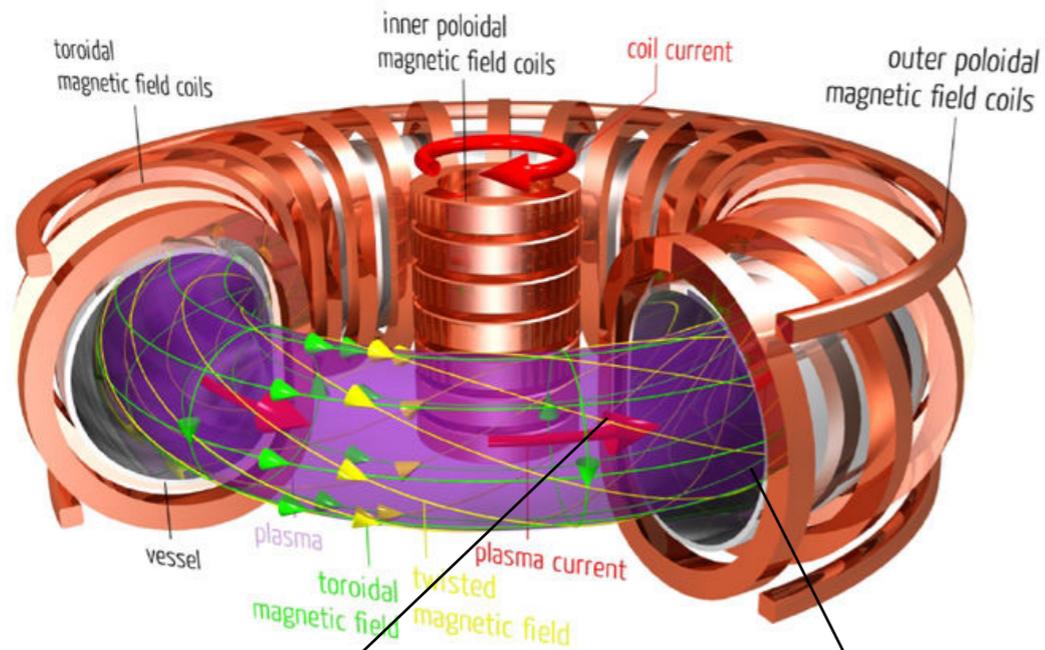
Doctor Octopus in Spider man I



# Laboratory plasmas

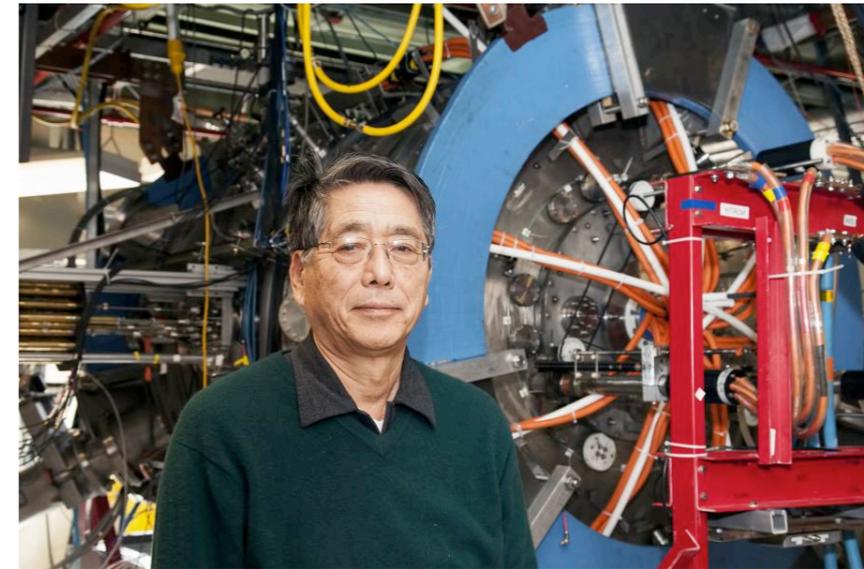
## Fusion device

e.g., ITER Tokamak @ France



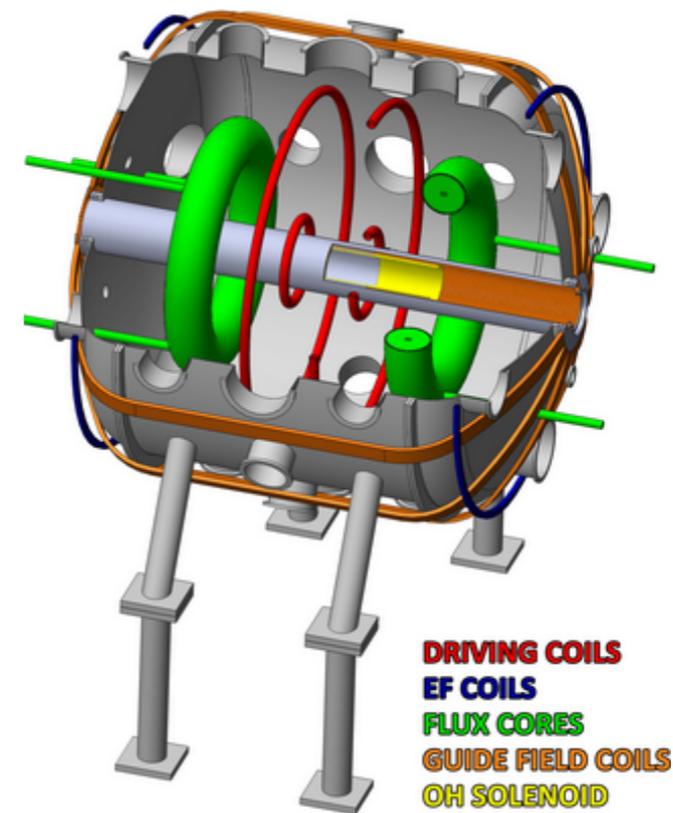
## Reconnection Experiment

MRX @ PPPL



FLARE @ PPPL

TREX @  
U. Wisconsin



LAPD @  
UCLA

- Reconnection causes the Sawtooth crashes in Tokamak!



# Honey, I Blew Up the Tokamak



[+ Play Audio](#) | [+ Download Audio](#) | [+ Join mailing list](#)

**August 31, 2009:** Magnetic reconnection could be the Universe's favorite way to make things explode. It operates anywhere magnetic fields pervade space--which is to say almost everywhere. On the sun magnetic reconnection causes solar flares as powerful as a billion atomic bombs. In Earth's atmosphere, it fuels magnetic storms and auroras. In laboratories, it can cause big problems in fusion reactors. It's ubiquitous.

Top

1

2

3

4

**Fundamental problems & research**

## 1/2. Reconnection Rate Problem

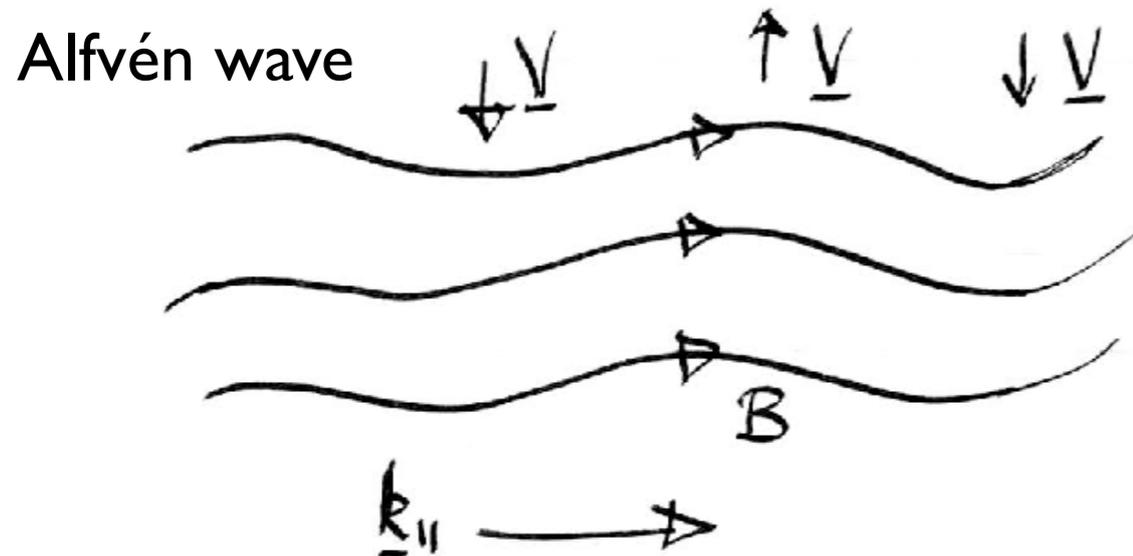
- How quickly can reconnection process magnetic flux?

# Magnetic tension & Alfvén waves

magnetic tension:  $\frac{\mathbf{B} \cdot \nabla \mathbf{B}}{4\pi}$

$$\frac{B_y(\partial_y B_x)}{4\pi} \hat{x}$$

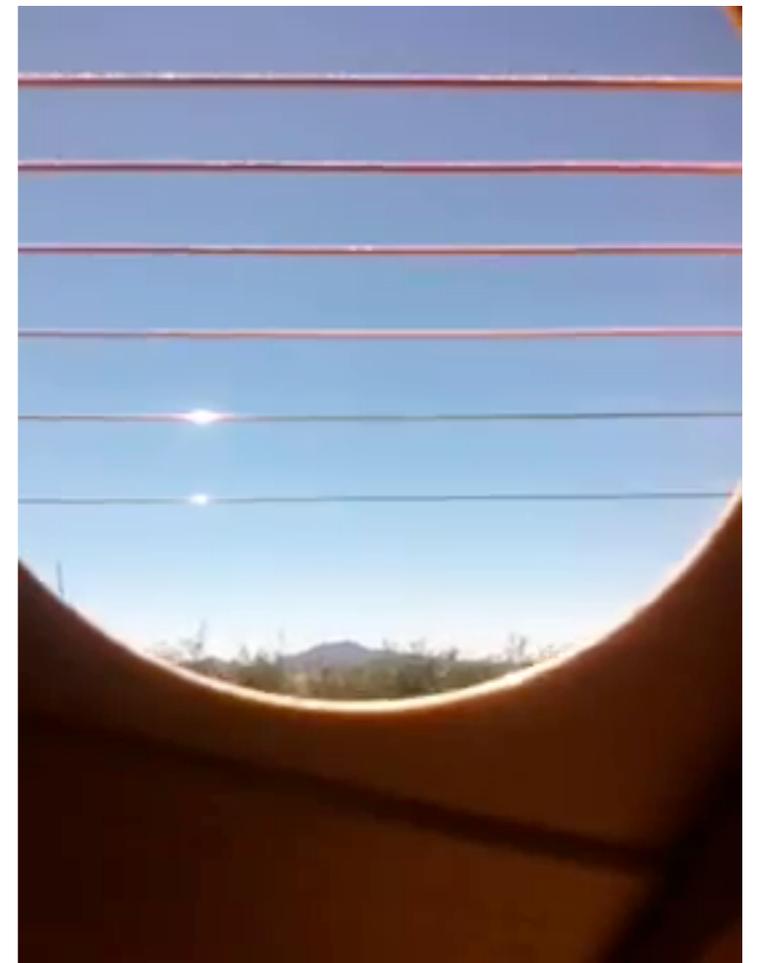
plasma inertia:  $nm_i \frac{d\mathbf{V}}{dt}$



Alfvén speed

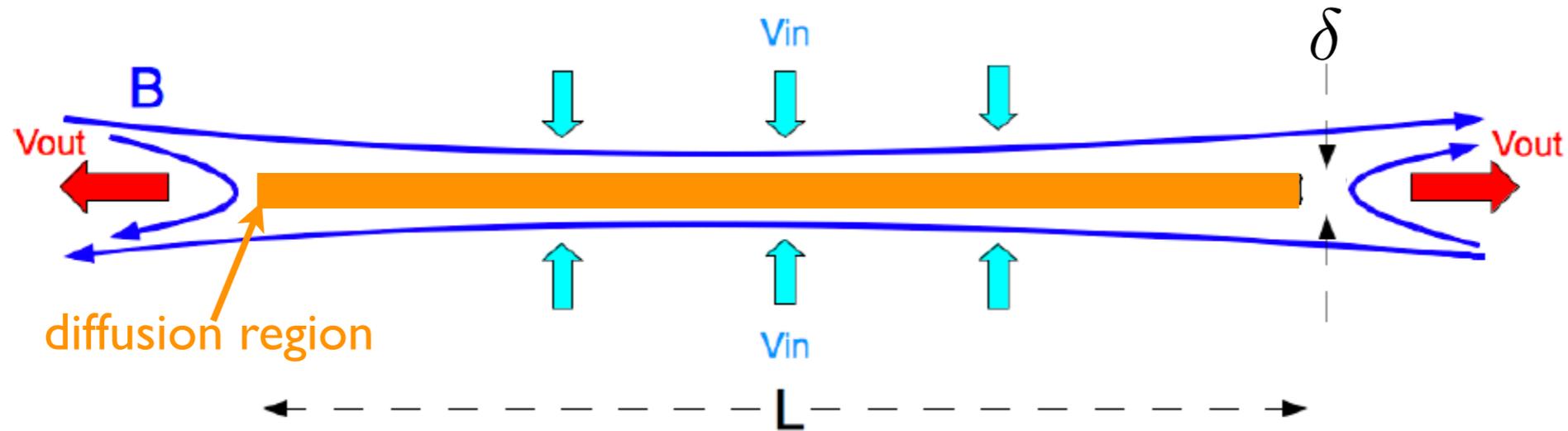
$$\rightarrow V_A \sim \frac{B}{\sqrt{4\pi nm_i}}$$

vibration of guitar strings



(Youtube: iphone 4 inside a guitar oscillation! VERY COOL!)

# Sweet-Parker solution (1957)



mass conservation:  $\nabla \cdot (n\mathbf{V}) \simeq 0 \quad \rightarrow V_{in}L \simeq V_{out}\delta$

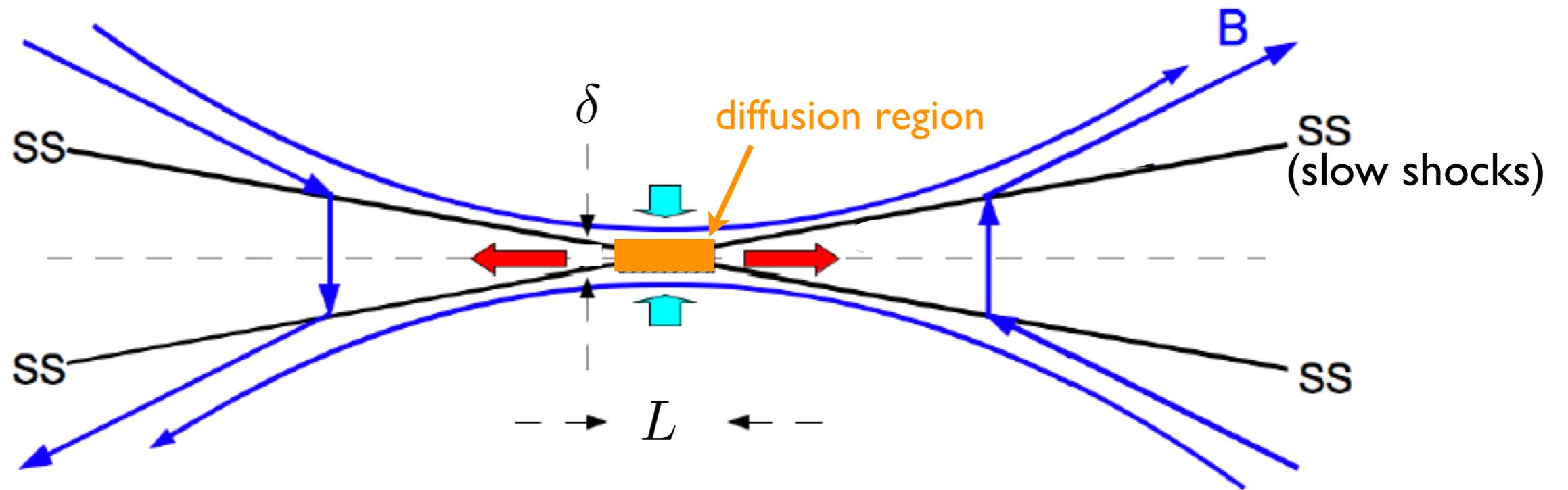
momentum eq.:  $\frac{\mathbf{B} \cdot \nabla \mathbf{B}}{4\pi} \simeq nm_i \mathbf{V} \cdot \nabla \mathbf{V} \quad \rightarrow V_{out} \simeq \frac{B}{\sqrt{4\pi nm_i}} = V_A !$

tension                      inertia

normalized reconnection rate  $\rightarrow R \equiv \frac{V_{in}}{V_A} \sim \frac{\delta}{L}$

- **However**, this model has a small  $\delta/L$ , the rate is too small to explain the time-scales in solar flare. (Parker 1963)
- To explain the flares, it requires  $R \sim 0.1$ . (Parker 1973)

# Petschek solution (1964)

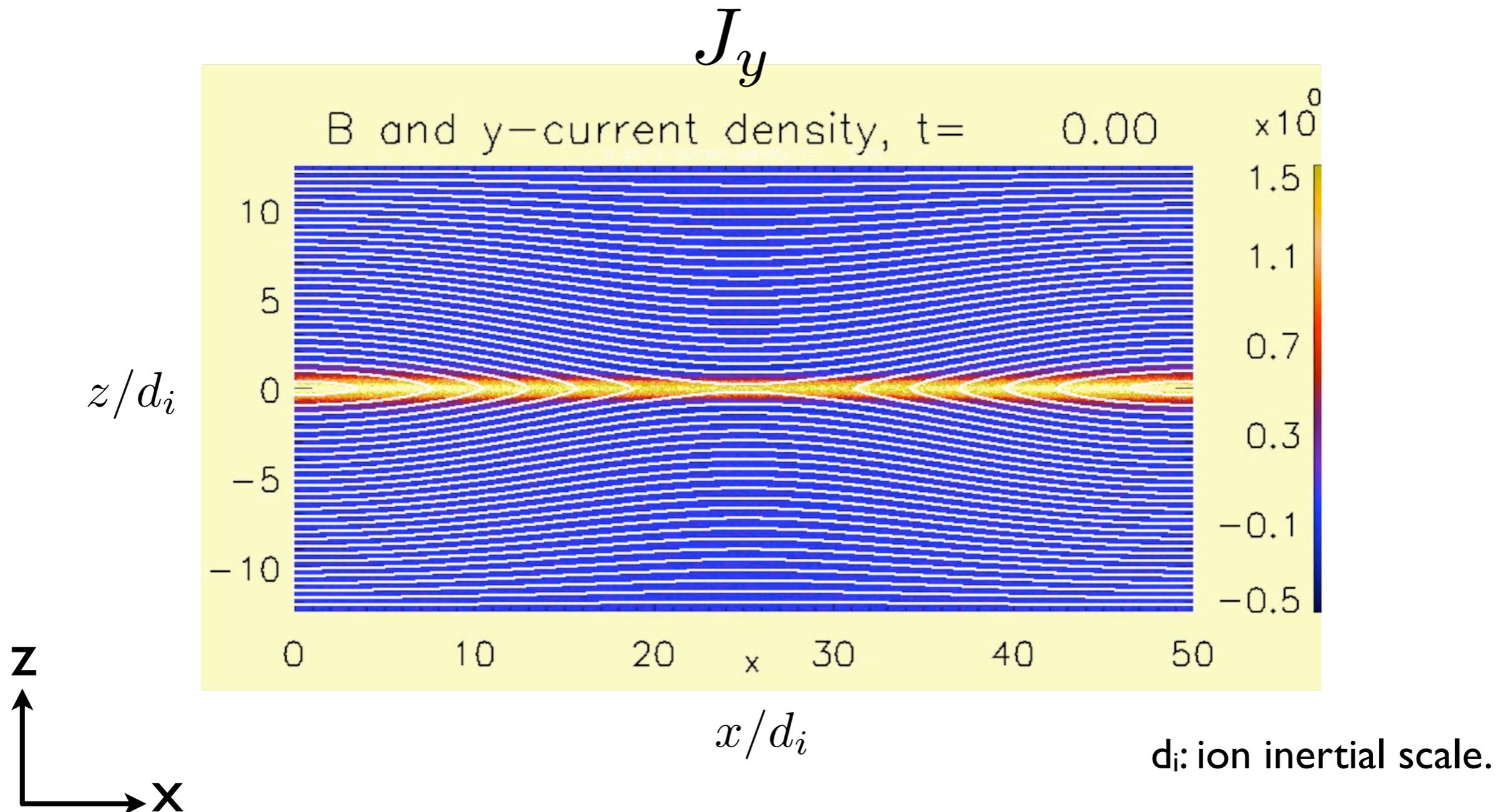


Reconnection rate is much larger because  $R \sim \frac{\delta}{L} \uparrow$

- **However**, this is not a self-consistent solution. (Sato & Hayashi, 79; Biskamp, 86)

\*aspect ration  $\equiv$  aspect ratio of the diffusion region

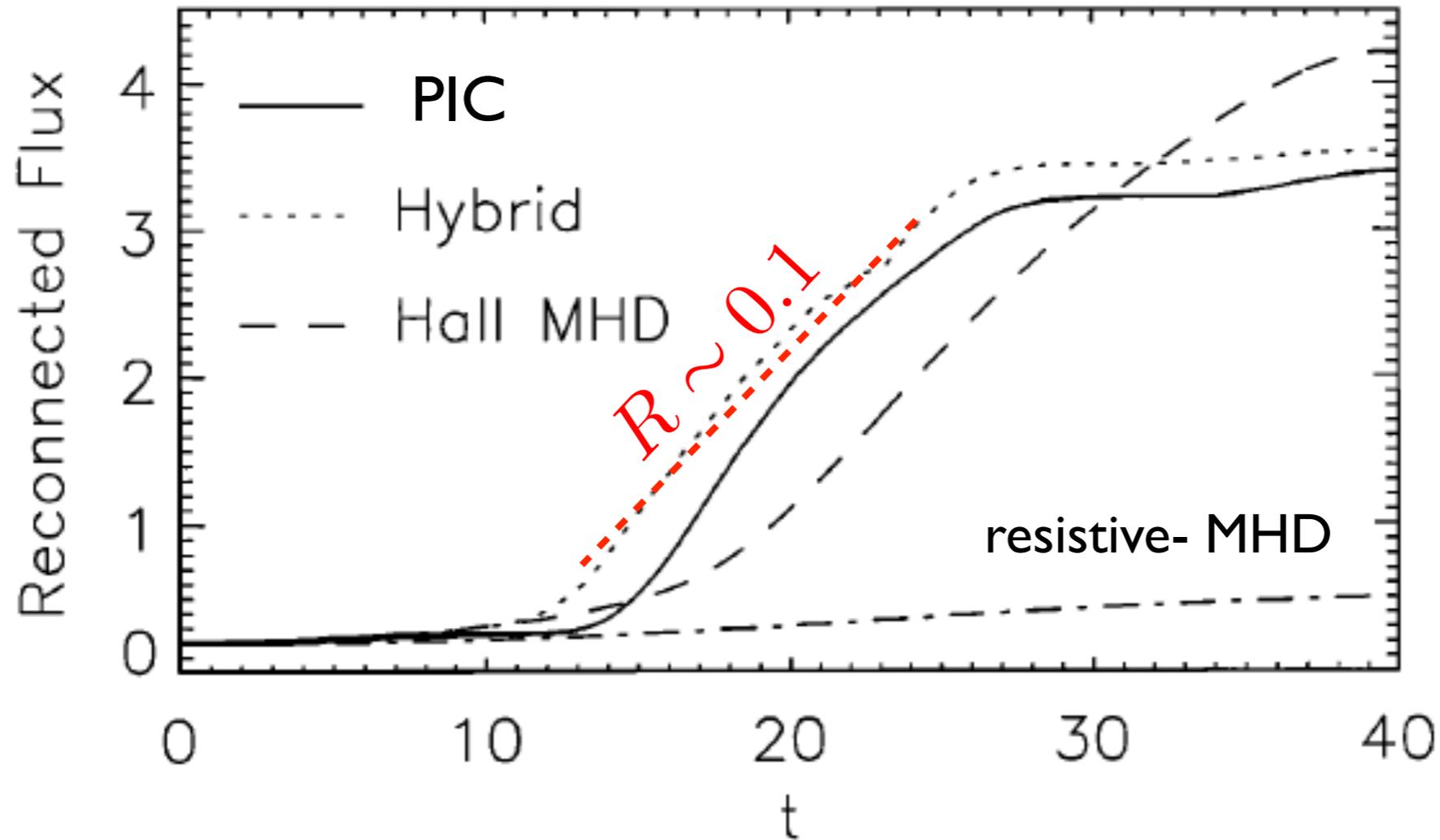
# Reconnection in particle-in-cell (PIC) simulations



- The diffusion region is localized like the Petschek solution.
- Why PIC? Why not using magnetohydrodynamics (MHD)?
  - because PIC captures the key physics that breaks the frozen-in condition in nature.

# GEM Reconnection Challenge (2001)

(Birn et al. 2001)



\* the importance of Hall term in Ohm's Law was debated for the past 16 years.  
(Sonnerup 79)

- A similar reconnection rate  $R \sim 0.1$  is reported in most models & over a wide parameter range!

To be solved.

Q: Why is the fast reconnection rate order 0.1 in disparate systems?

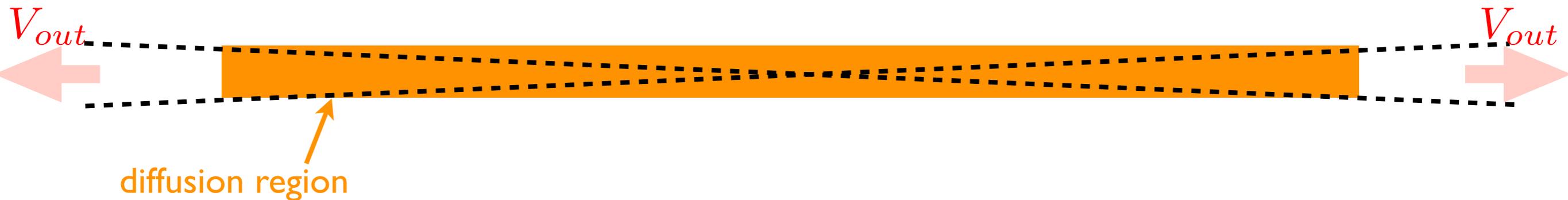
-- including PIC, hybrid, Hall-MHD, MHD with a localized resistivity...etc

\*clue: can not be the diffusion-scale physics!

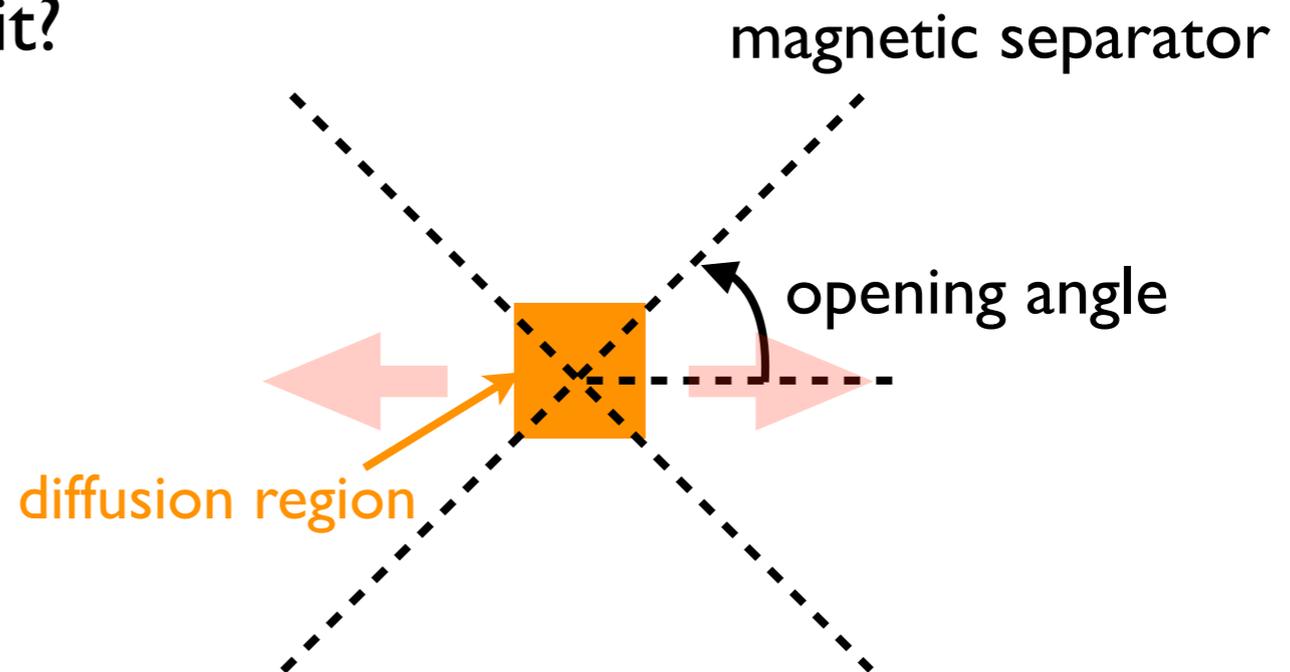
# Explanation of rate $\sim 0.1$

-- Geometrical consideration!

In the small  $\delta/L$  limit,  $R \sim \delta/L \rightarrow 0$



How about the large  $\delta/L$  limit?



It turns out that when  $\delta/L \rightarrow 1$ ,  $R \rightarrow 0$  !

-- Hey~ then there should be an optimized  $R_{max}$  in between!

-- This  $R_{max}$  may explain the value 0.1 !

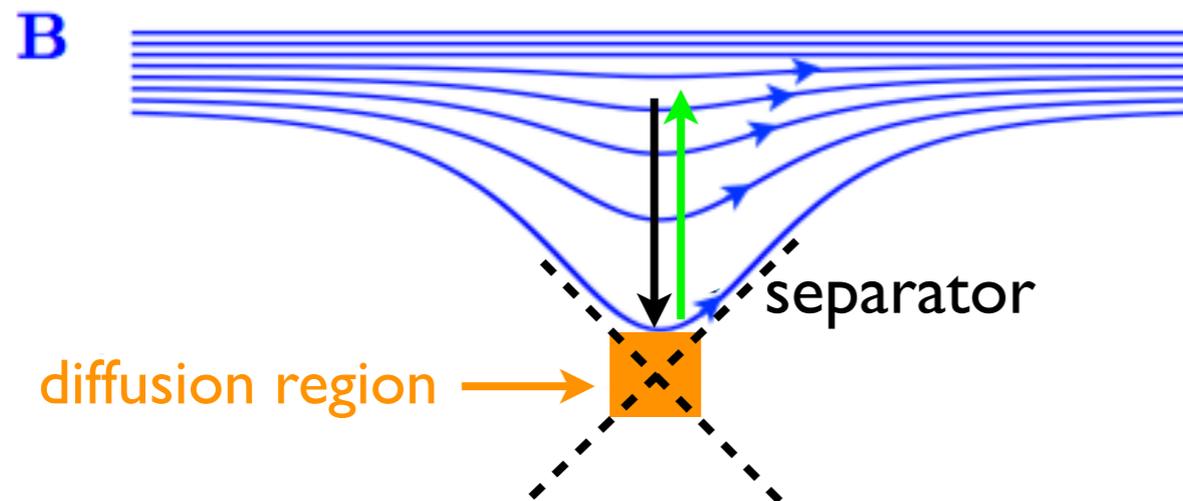
# Explanation of rate $\sim 0.1$

-- Geometrical consideration!

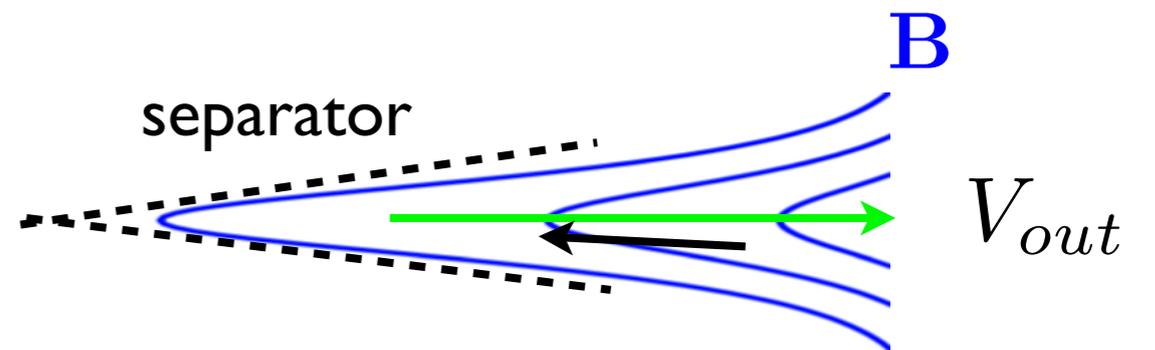
In the large  $\delta/L$  limit .....

$$\frac{\text{tension}}{4\pi} \frac{\mathbf{B} \cdot \nabla \mathbf{B}}{4\pi} \simeq \frac{\text{magnetic pressure}}{8\pi} \frac{\nabla(B^2)}{8\pi} + \text{inertia} \quad + \quad nm_i \mathbf{V} \cdot \nabla \mathbf{V}$$

@ inflow region



@ outflow region



→ decrease the reconnecting field!!!

→  $R \downarrow$

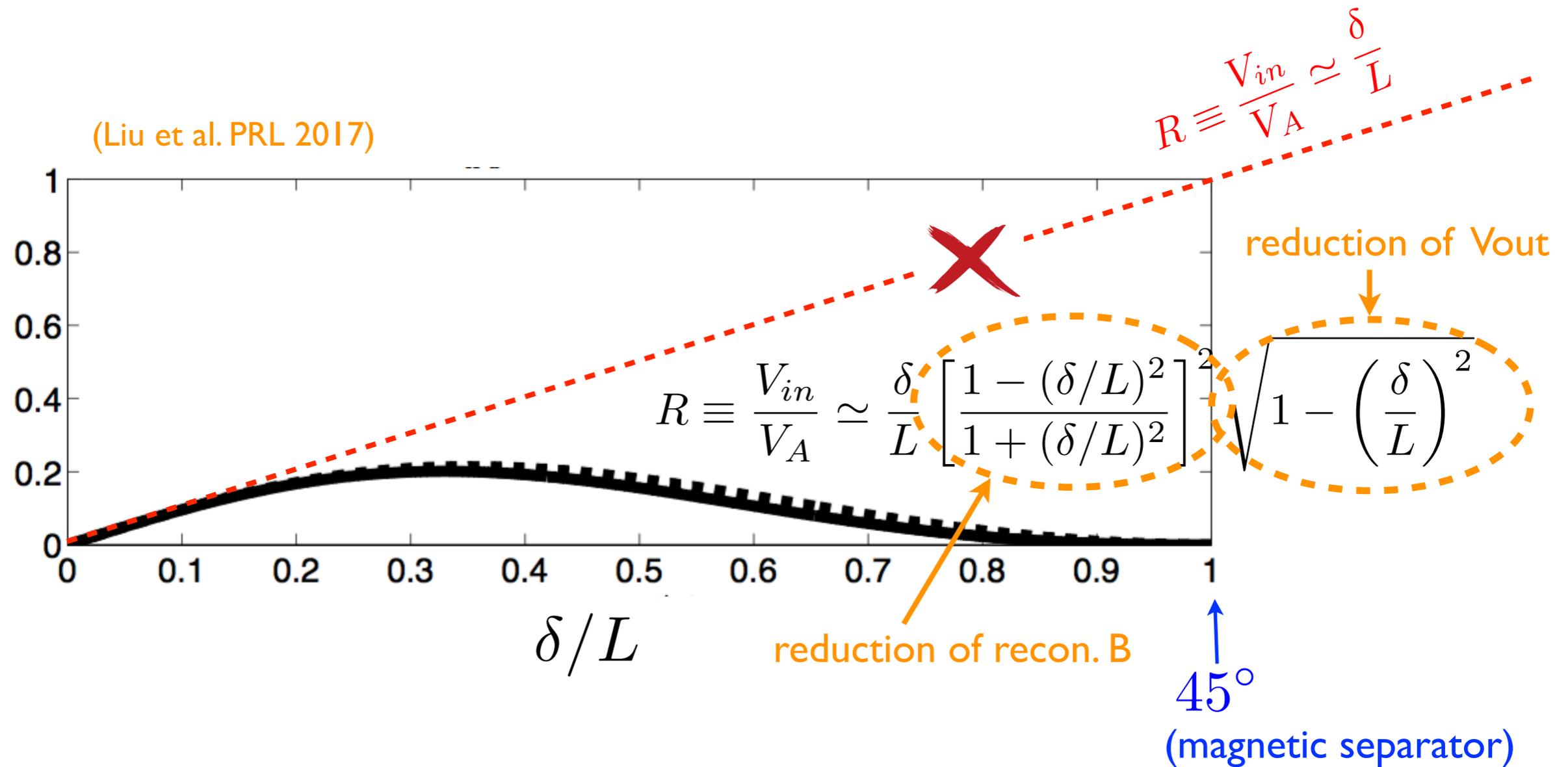
→ decrease the outflow speed!!!

→  $R \downarrow$

- Constraints imposed at the inflow & outflow region (upper) bound the rate!

# Explanation of rate $\sim 0.1$

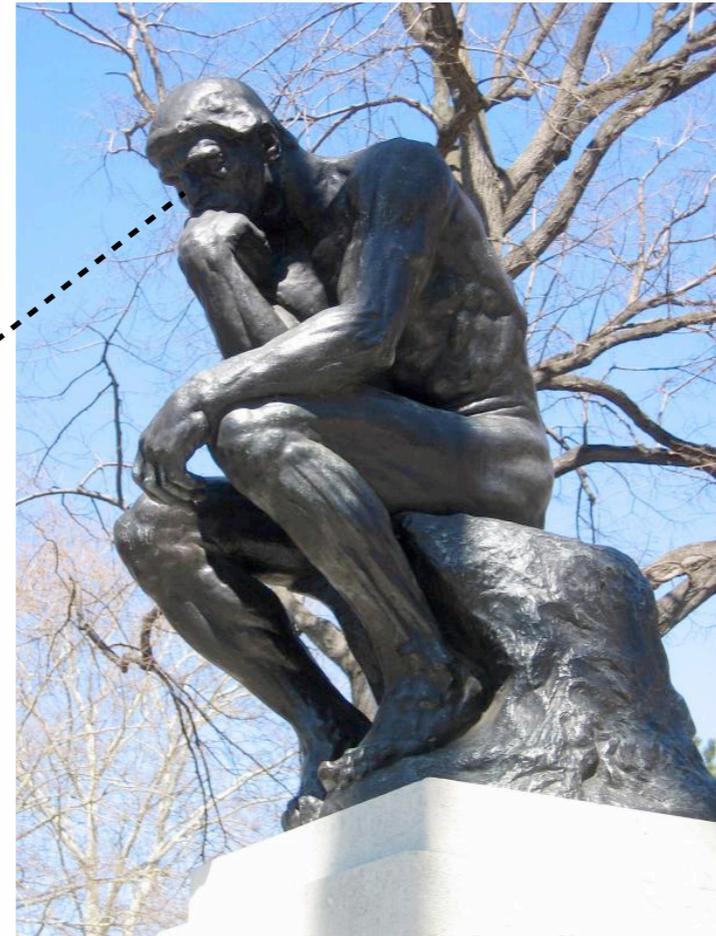
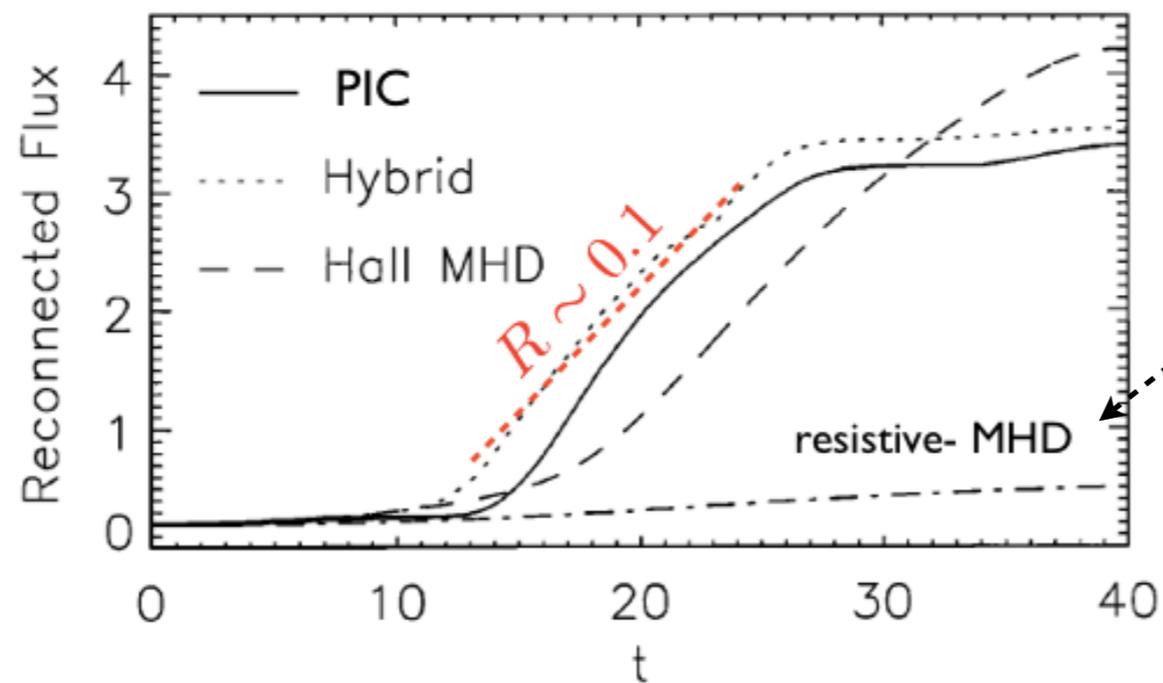
-- Geometrical consideration!



- Reconnection tends to proceed near the most efficient state with  $R \sim O(0.1)$ . ✓
- Nicely, rate is insensitive to  $\delta/L$  near this state. ✓

Q1: Why fast rate  $R \sim O(0.1)$ ? ✓

Q2: Why is reconnection slow in the resistive-MHD case?

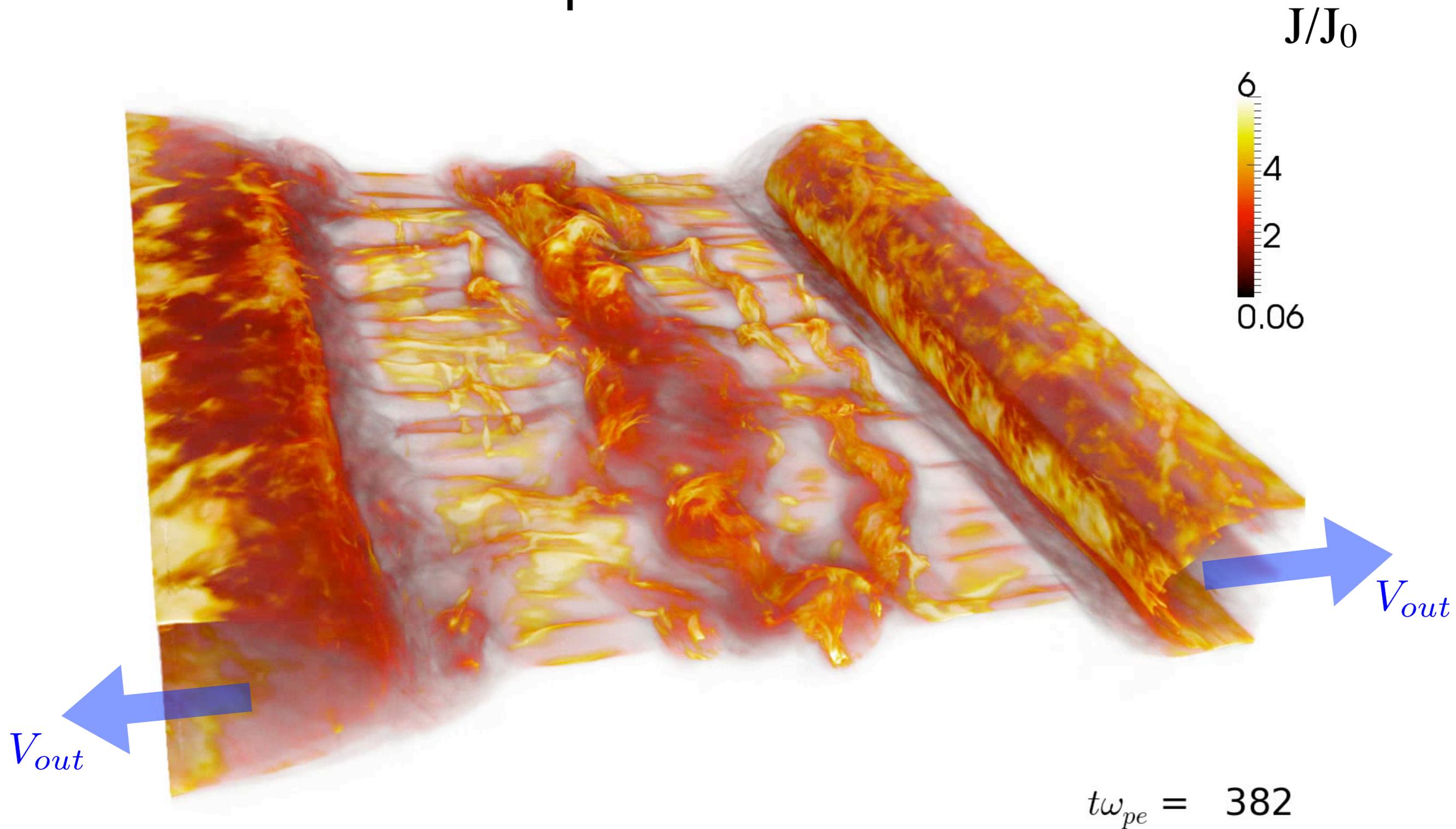


requires more thinking...

## 2/2. Three- dimensional nature of reconnection

- How about the freedom coming from the extra dimension?

# An example 3D simulation



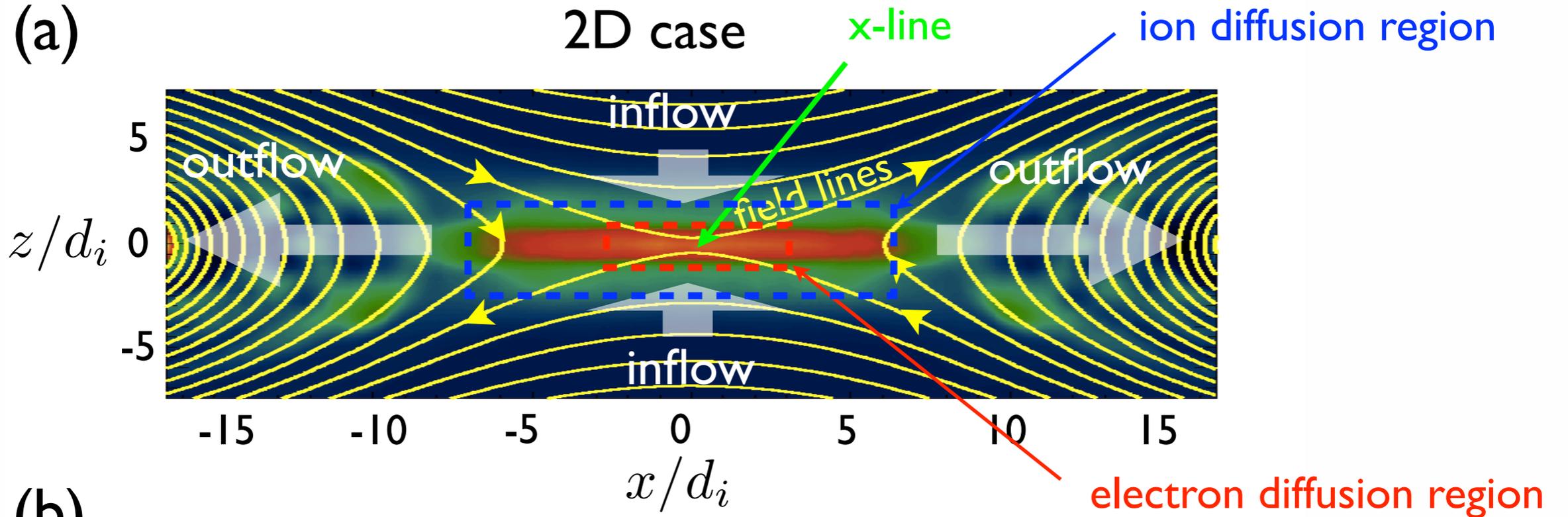
Distinct 3D features, including

- flux ropes.
- kink instability.
- turbulence.

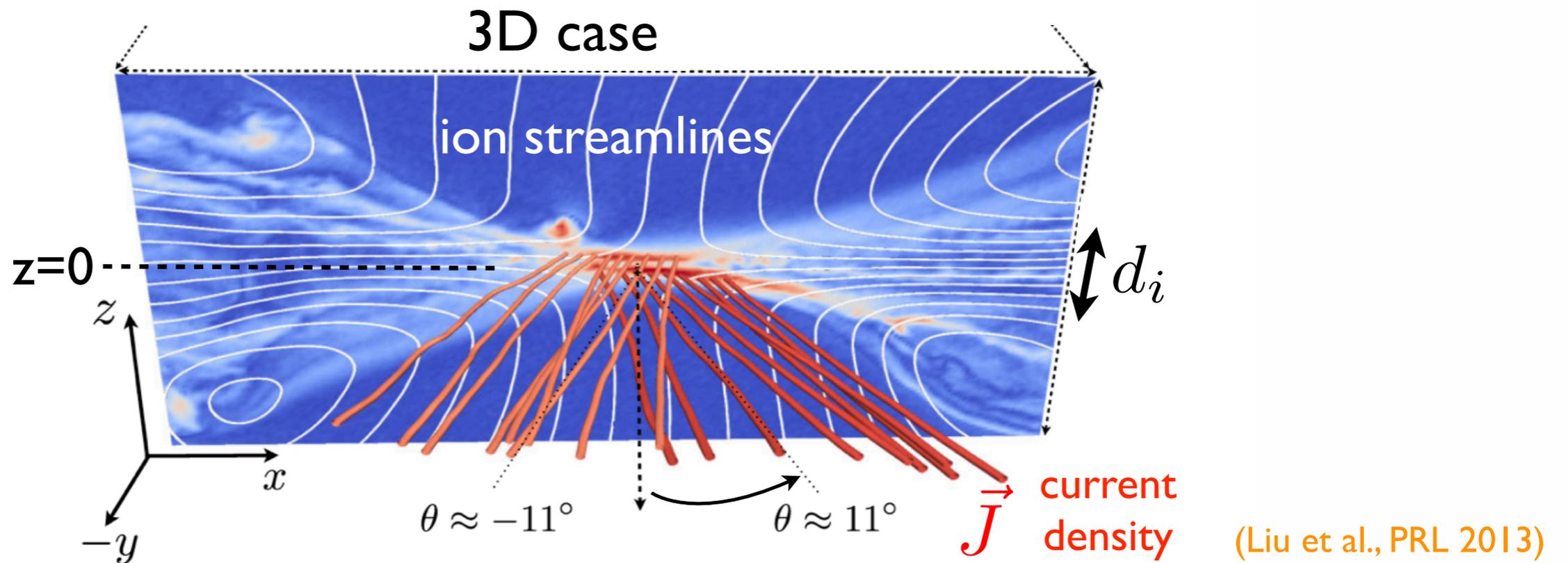
$$t\omega_{pe} = 382$$

# 3D diffusion region can be fundamentally different!!

(a)



(b)

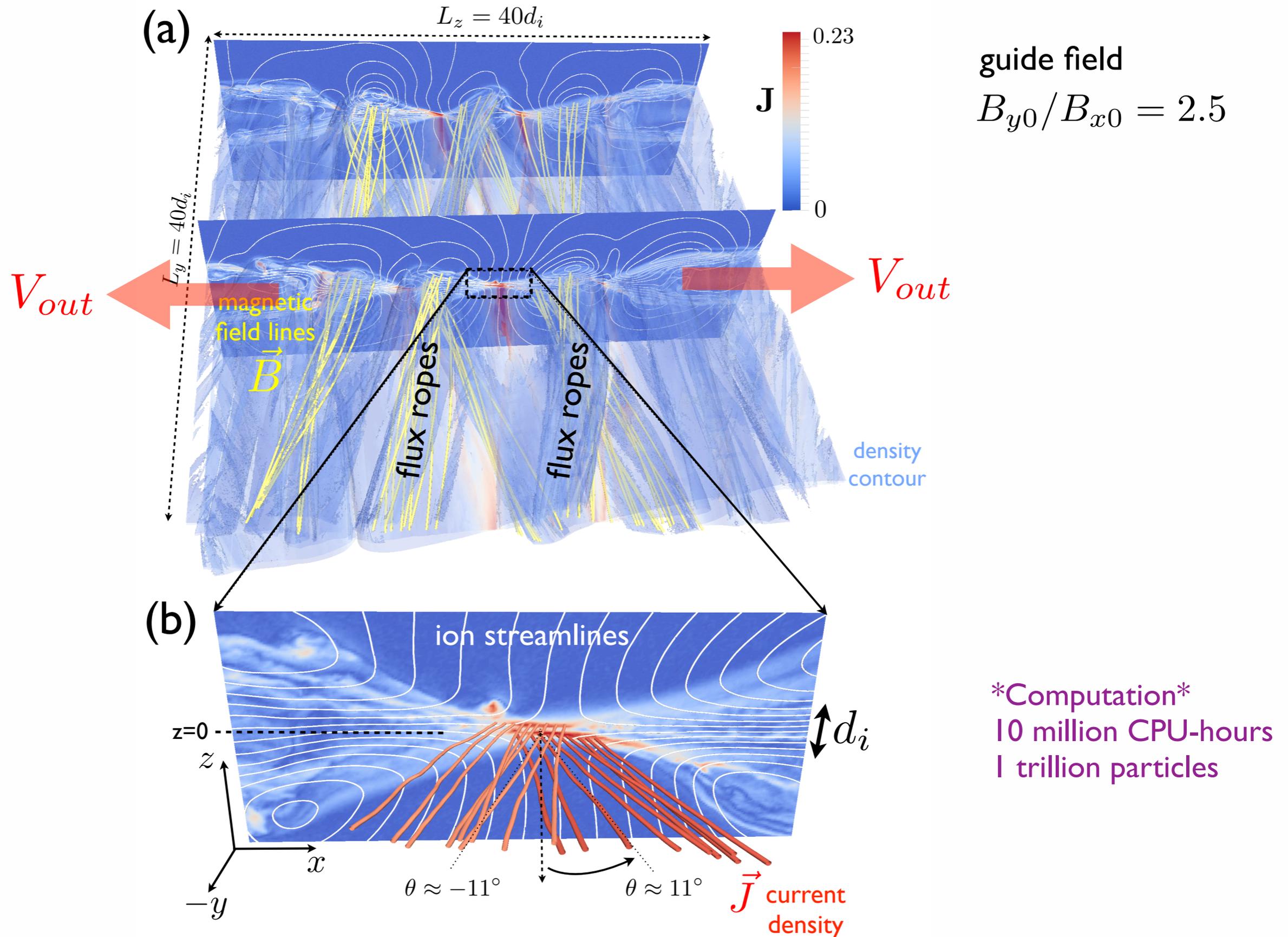


Q: What is causing this? consequence?

To be solved.

Q: What is causing the bifurcation of electron diffusion region?

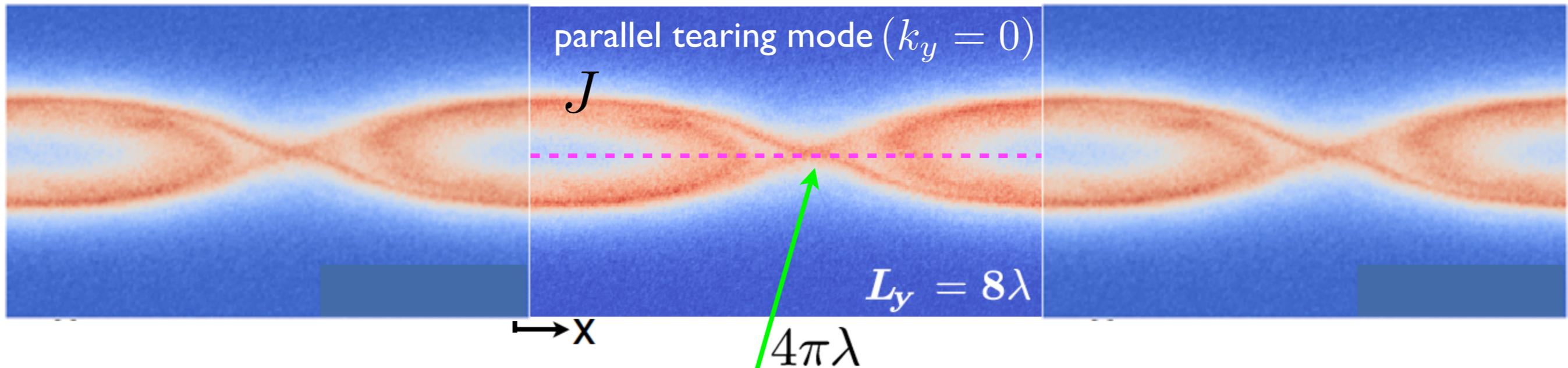
# Global structure



\*clue: bifurcated layer is located in between these intertwined flux ropes.  
 & tearing modes give rise to these flux ropes!

# Explanation of the bifurcation

-- oblique tearing modes!



Resonant surfaces @  $\mathbf{k} \cdot \mathbf{B} = 0$

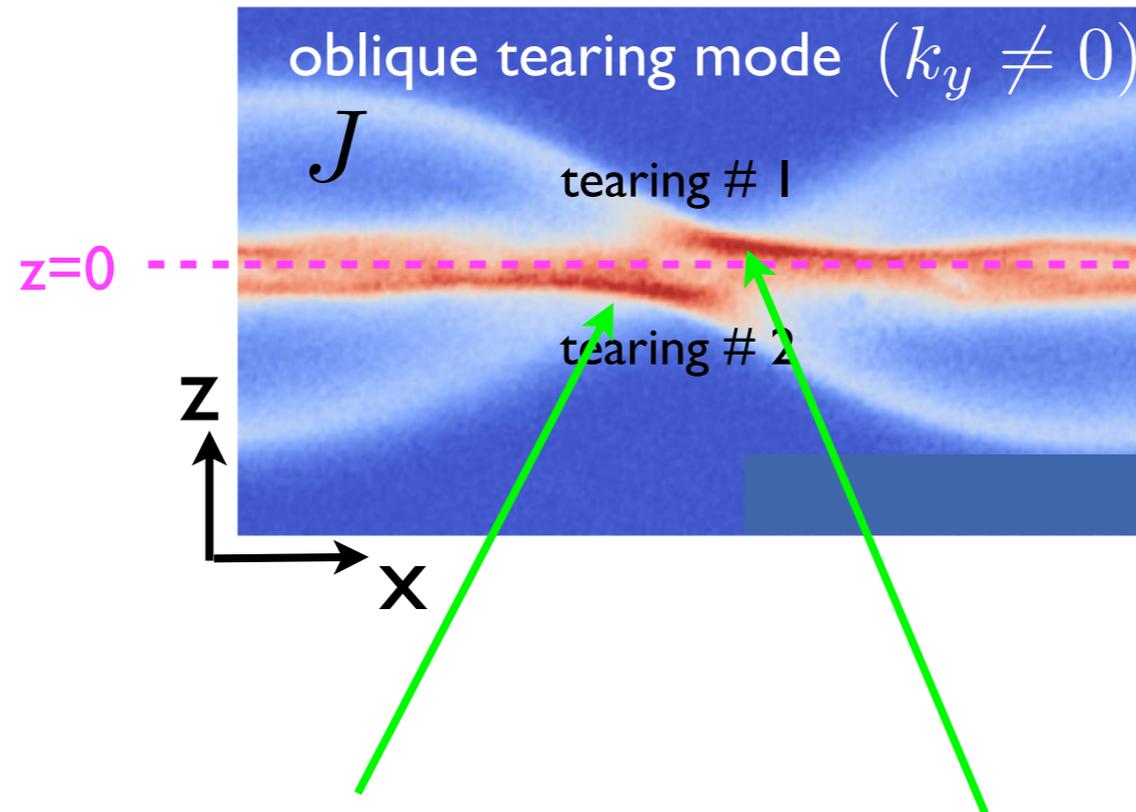
initial thickness  $\rightarrow \frac{z_s}{\lambda} = -\tanh^{-1} \left( \frac{k_y B_{y0}}{k_x B_{x0}} \right)$

$$\theta \equiv \tan(k_y/k_x)$$

- 2D only allows the parallel tearing mode. i.e., no bifurcation.

# Explanation of the bifurcation

-- oblique tearing modes!



Resonant surfaces @  $\mathbf{k} \cdot \mathbf{B} = 0$

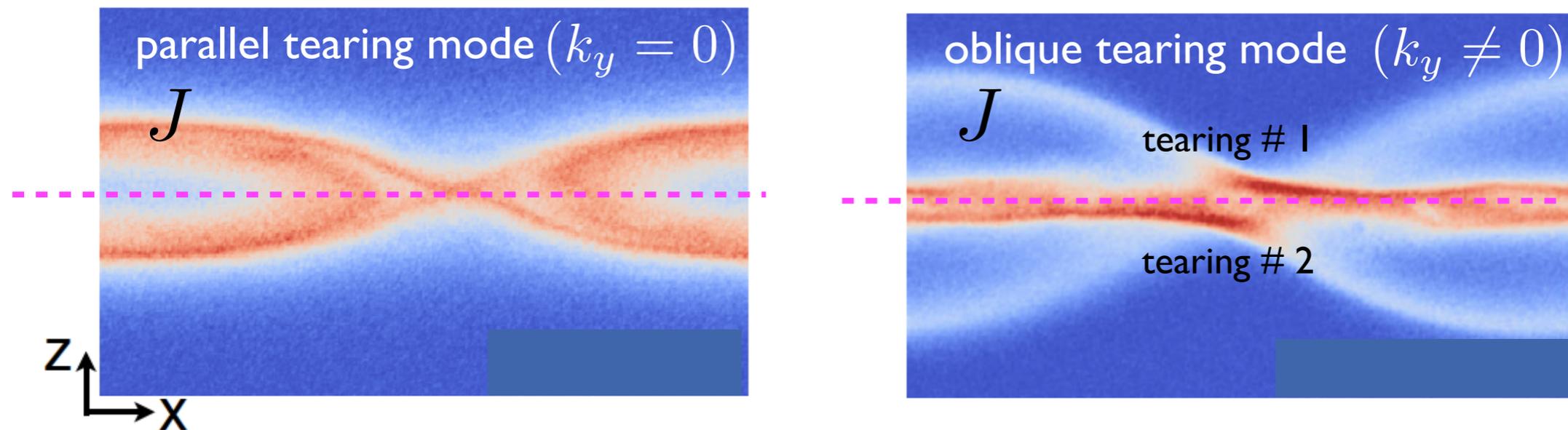
$$\frac{z_s}{\lambda} = -\tanh^{-1} \left( \frac{k_y B_{y0}}{k_x B_{x0}} \right)$$

$$\theta \equiv \tan(k_y/k_x)$$

- 3D allows a spectrum of oblique tearing modes, unlike 2D.

# Explanation of the bifurcation

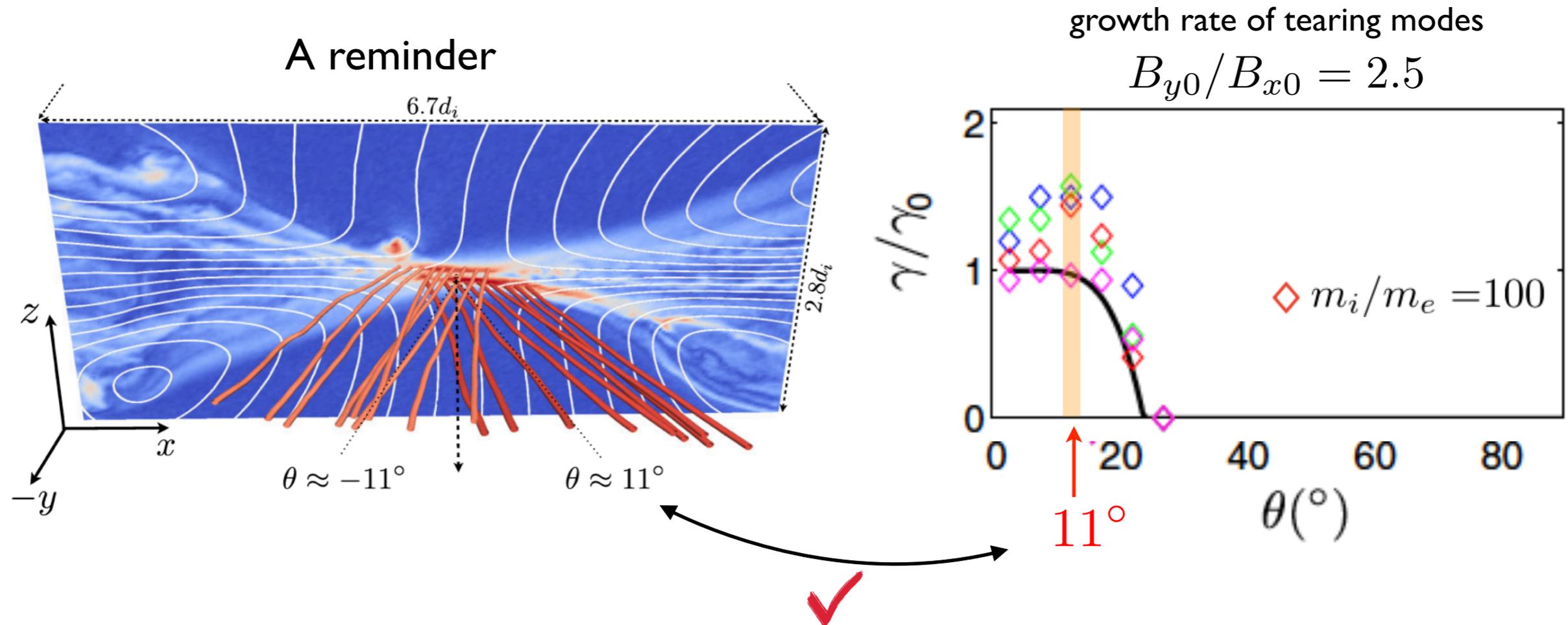
-- oblique tearing modes!



- **Bifurcated or Not**, depends on the competition between oblique & parallel tearing modes!

# Explanation of the bifurcation

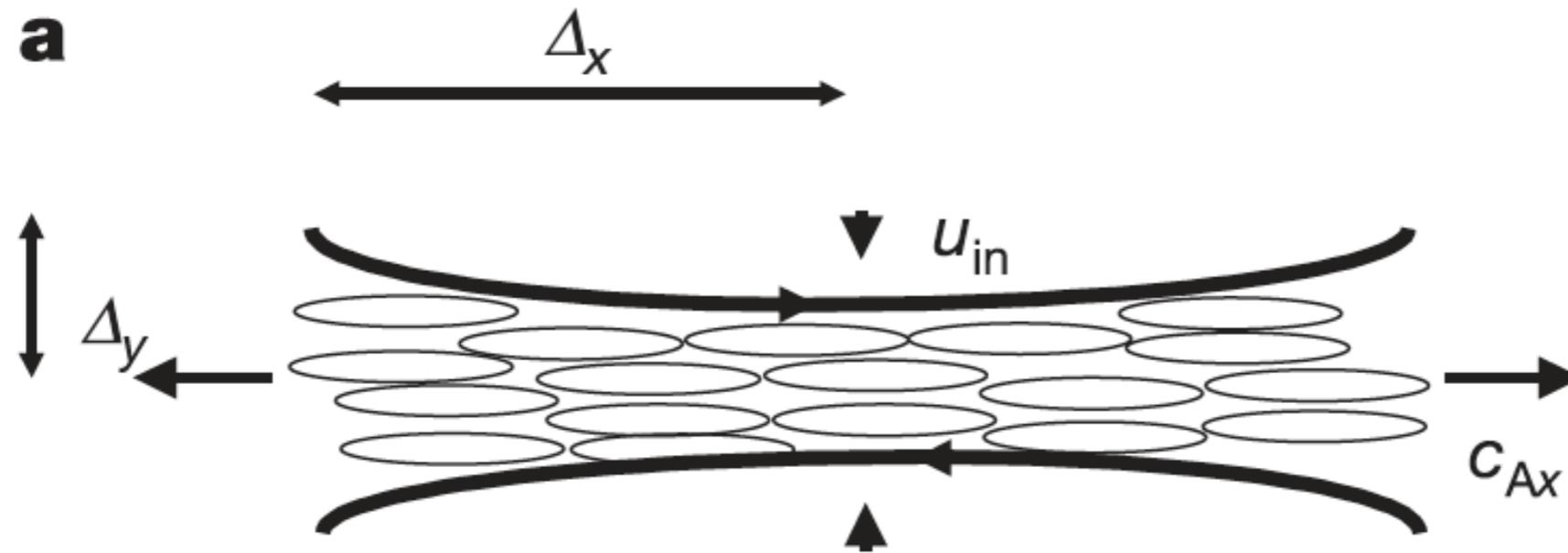
-- oblique tearing modes!



- The most unstable tearing mode should dominate!!
- Theory predicts that the oblique mode dominates when  $B_{y0}/B_{x0} > 1$ . ✓

# Open Questions

With a thicker current sheet, like that in the solar flare



(Drake et al., NATURE 2006)

Lots of resonant surfaces are possible!

Q: How do these oblique tearing modes interact & volume-fill the current sheet?

Q: Reconnection rate? Energy dissipation? Particle acceleration??

(Fermi-type acceleration? or direct acceleration?)

# Summary

- Magnetic reconnection is an important energy release process in plasmas, and it is relevant in space, solar, astrophysical & laboratory plasmas.
- Reconnection rate problem & 3D nature of reconnection are discussed.
- Reconnection is relevant to many exciting on-going & future projects: [MMS](#), [Solar Prob +](#), [FLARE](#), [TREX](#), [LAPD](#), [ITER](#), [HAWC](#),.....etc.
- Nowadays, simulations and analytical techniques allow us to study a wide range of problems in plasmas physics.
- Lots of interesting problems; Lots of opportunities for students.



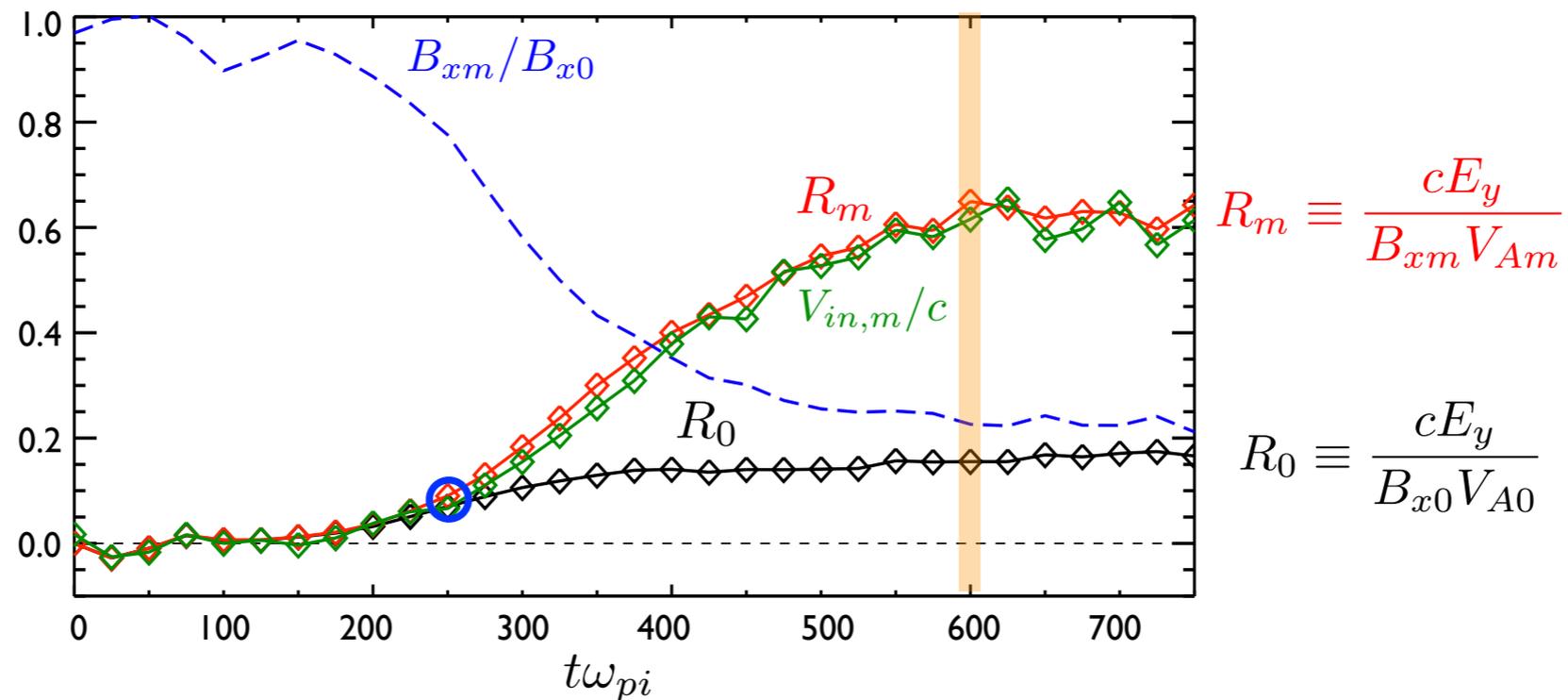
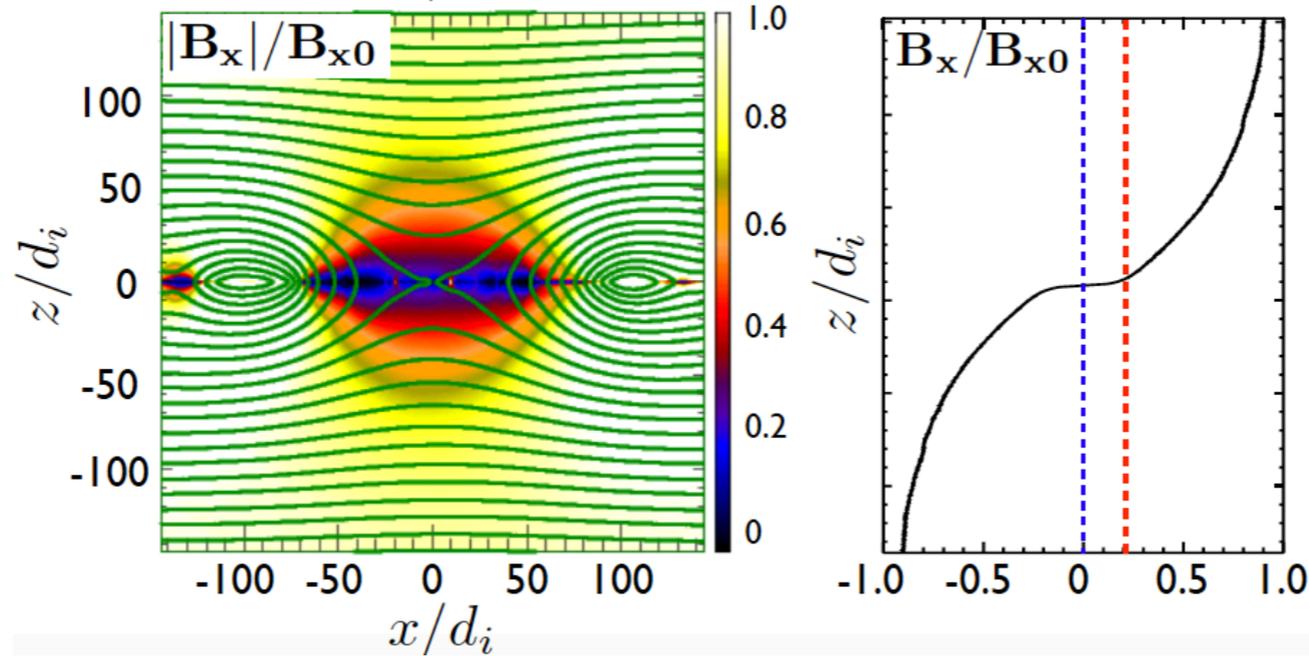








# An example run shows the imbedding effect



- Reduction of the reconnecting field immediately upstream of the diffusion region (micro-scale) is observed.
- Local reconnection rate  $R_0 \sim O(0.1)$  does not go up even when the micro-scale rate  $R_m$  goes up to  $\sim O(1)$ .

Let a fluid filament initially following the closed contour  $S$  be given and let  $\Phi$  be the initial flux of  $\mathbf{B}$  through it. A short interval  $dt$  later, each element  $d\mathbf{l}$  of the contour will have been displaced by an amount  $\mathbf{v} dt$ , sweeping in the process an area  $(\mathbf{v} \times d\mathbf{l}) dt$  (Figure 1). In this time interval,  $\Phi$  changes by an amount  $d\Phi$ , ascribable

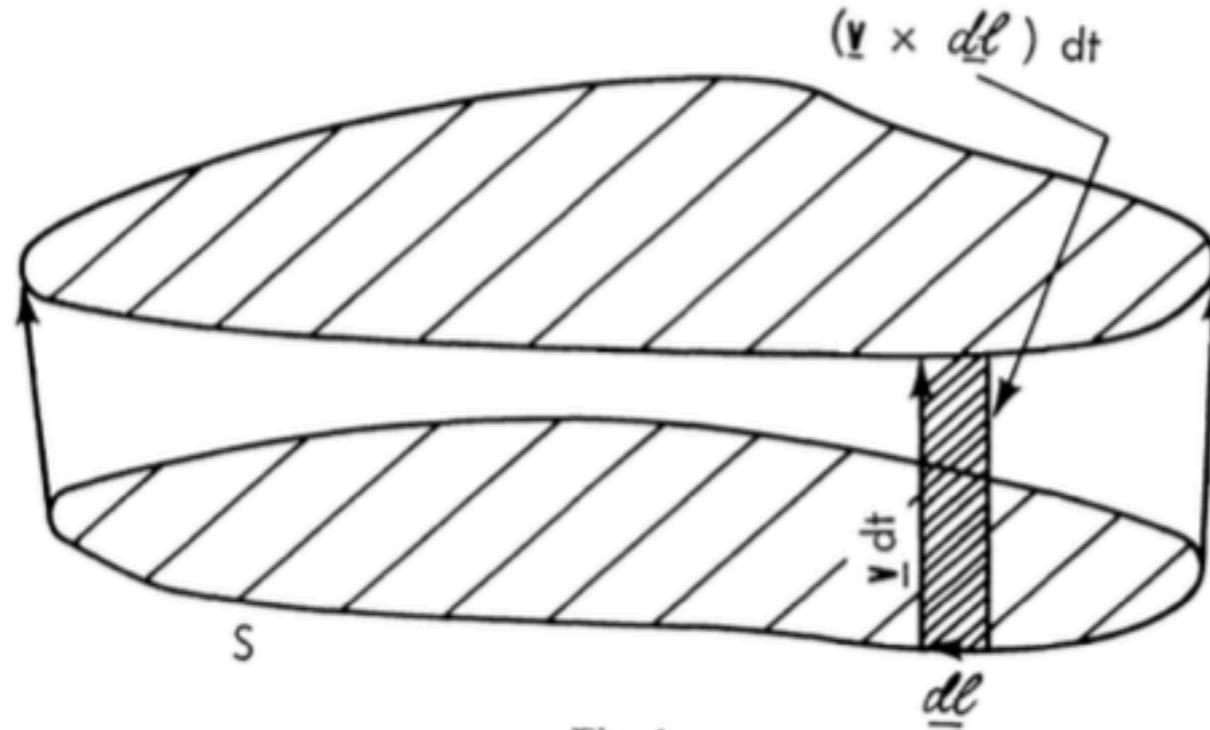


Fig. 1.

to two causes. The time variation of the field contributes the surface integral

$$\int_s \frac{\partial \mathbf{B}}{\partial t} \cdot d\mathbf{A} dt \quad (4-4)$$

while the variation of the area bounded by the filament adds the flux through the area swept by it (Figure 1), equaling

$$\oint \mathbf{B} \cdot (\mathbf{v} \times d\mathbf{l}) dt = - \int \nabla \times (\mathbf{v} \times \mathbf{B}) \cdot d\mathbf{A} dt \quad (4-5)$$

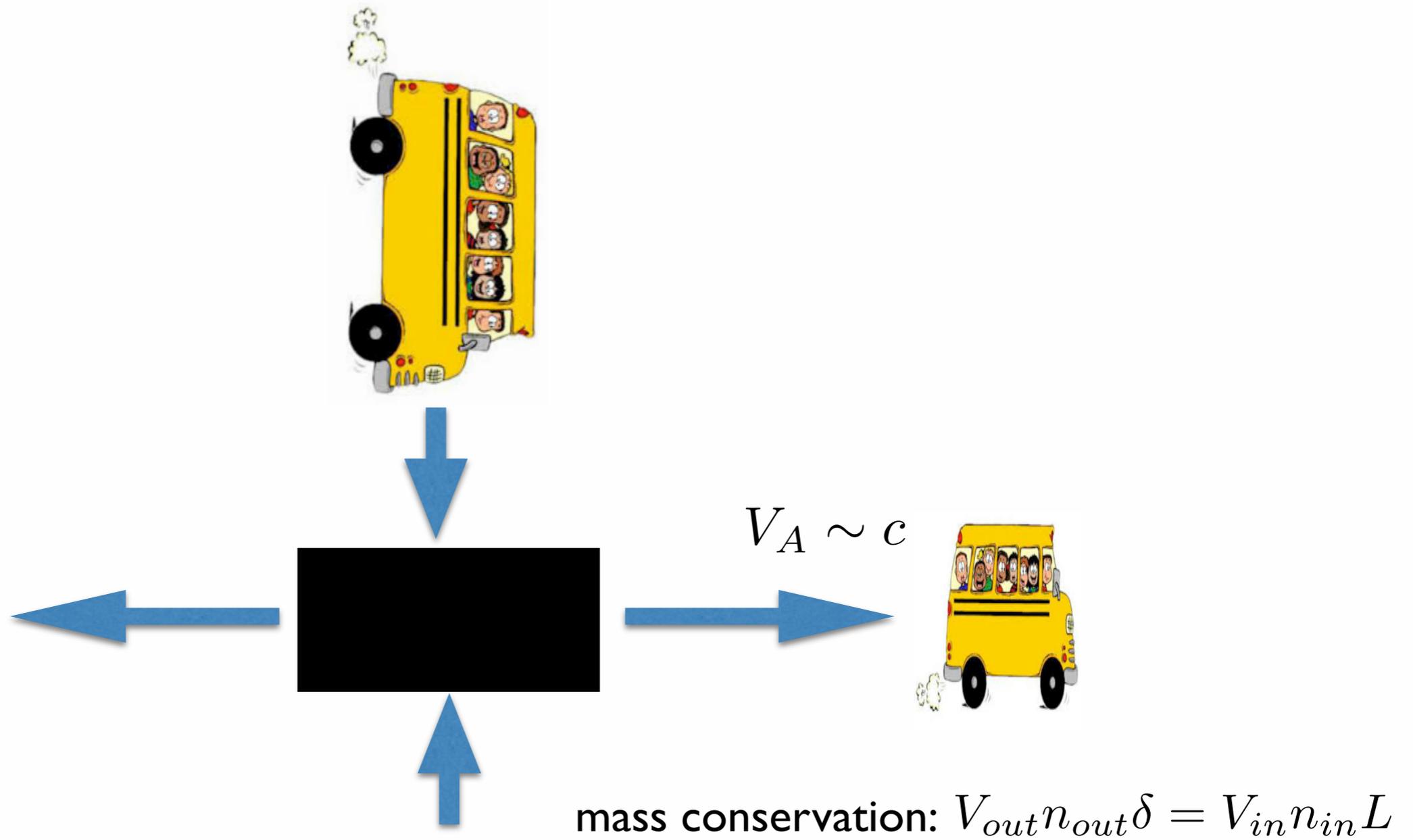
Thus

$$d\Phi = \int \left( \frac{\partial \mathbf{B}}{\partial t} - \nabla \times (\mathbf{v} \times \mathbf{B}) \right) \cdot d\mathbf{A} dt \quad (4-6)$$

Combined with  
Faraday's law

$$d\Phi = 0 \quad (\text{Frozen-in}) \quad \text{if} \quad \mathbf{E} + \frac{\mathbf{v} \times \mathbf{B}}{c} = \nabla P$$

# Q: How could special relativity affect reconnection?

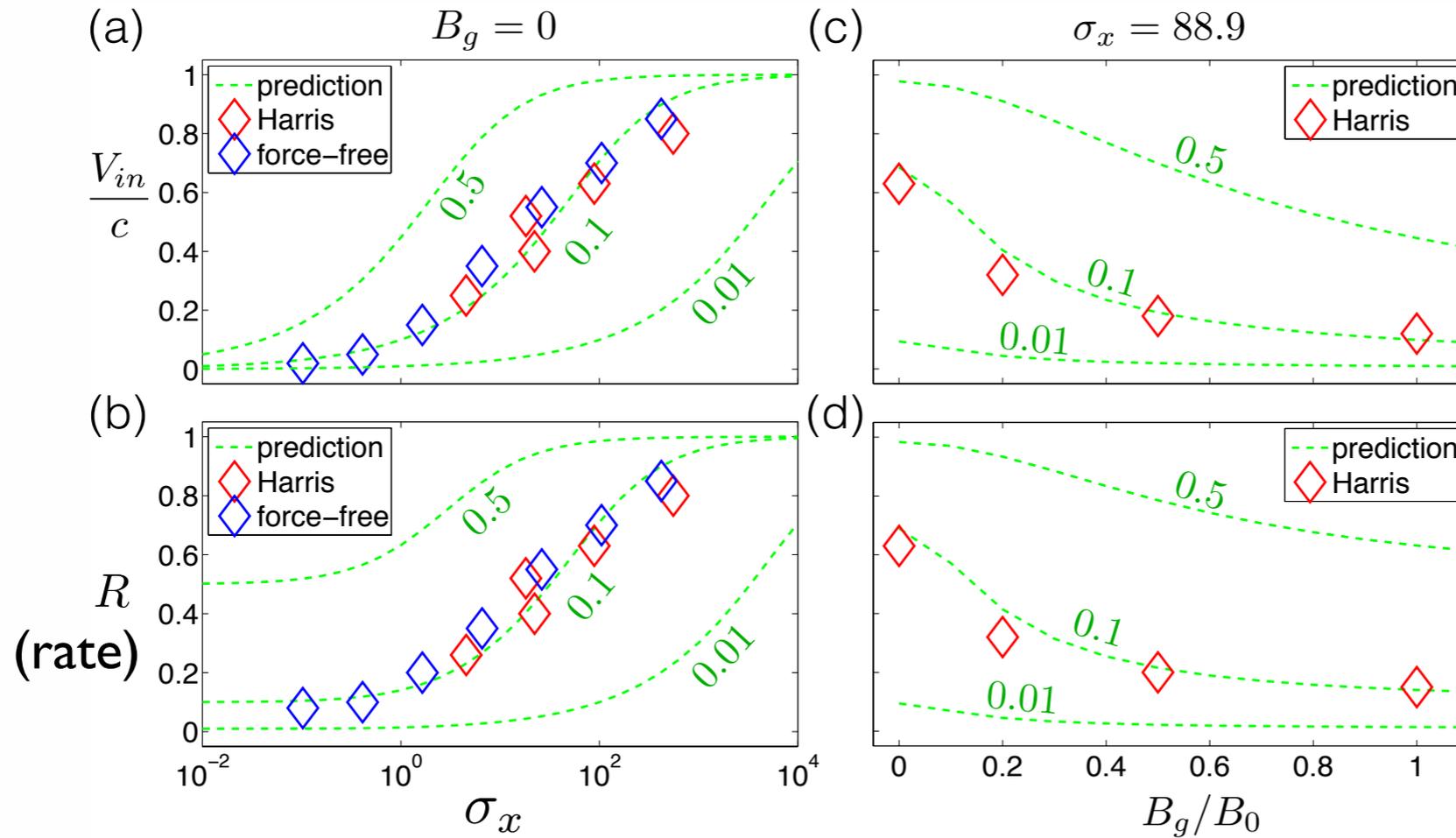


Alfven Speed:  $\frac{V_A}{c} = \sqrt{\frac{\sigma}{1 + \sigma}}$  (e.g., Anile 1989)

Magnetization param:  $\sigma = \frac{B^2}{8\pi w}$       Enthalpy:  $w = n'_e m_e c^2 + \frac{\Gamma}{\Gamma - 1} P'_e$

- Reconnection rate can be enhanced?

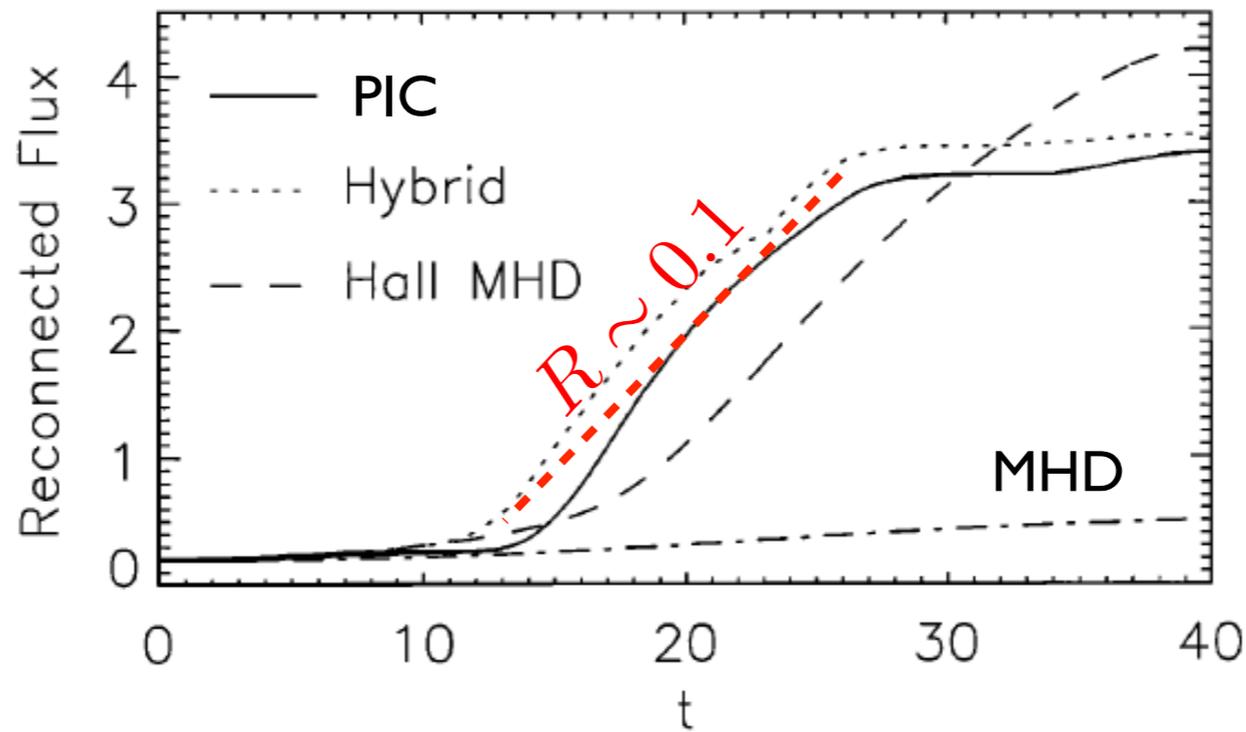
# Scaling of micro-scale inflow speed & reconn. rate



- Lorentz contraction + geometry factor  $\sim 0.1$  (Liu et al., PRL 2015)

$$\rightarrow \frac{V_{in}}{c} = 0.1 \sqrt{\frac{\sigma_x}{1 + \sigma_g + 0.01\sigma_x}}$$

# GEM Reconnection Challenge (2001)



(Birn et al., 2001)

Ohm's Law:  $V = RI$

Ohm's Law in plasmas:  $\mathbf{E} + \frac{\mathbf{v}_i \times \mathbf{B}}{c} = \eta \mathbf{J} + \frac{1}{nec} \mathbf{J} \times \mathbf{B} - \frac{1}{ne} \nabla \cdot \mathbf{P}_e + \frac{m_e}{e^2} \frac{d\mathbf{J}}{dt}$

Labels above the equation:  $\mathbf{E}$  (blue arrow), convection,  $\mathbf{v}_i \times \mathbf{B}$ , resis. (blue arrow), Hall term, pressure, inertia,  $\frac{1}{nec} \mathbf{J} \times \mathbf{B}$ ,  $-\frac{1}{ne} \nabla \cdot \mathbf{P}_e$ ,  $\frac{m_e}{e^2} \frac{d\mathbf{J}}{dt}$ .

MHD: ✓ slow

Hall MHD: ✓ ✓

Hybrid: ✓ ✓ ✓ fast

PIC: ✓ ✓ ✓

However, electron-positron (PIC):  
strong guide field limit (PIC):

✓  
✓  
✓

Q: Why is the fast rate  $R \sim 0.1$ ?